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# Exploiting Voltage Regulators to Enhance Various Power Attack Countermeasures

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**ABSTRACT** The security implications of on-chip voltage regulation on the effectiveness of various voltage/ frequency scaling-based countermeasures such as random dynamic voltage and frequency scaling (RDVFS), random dynamic voltage scaling (RDVS), and aggressive voltage and frequency scaling (AVFS) are investigated. The side-channel leakage mechanisms of different on-chip voltage regulator topologies are mathematically analyzed and verified with circuit level simulations. Correlation coefficient between the input data and monitored power consumption of a cryptographic circuit is used as the security metric to compare the impact of different on-chip voltage regulators when implemented with the aforementioned countermeasures. As compared to a cryptographic circuit without countermeasure, the RDVFS technique implemented with an on-chip switched-capacitor voltage converter reduces the correlation coefficient over 80 percent and over 92 percent against differential and leakage power analysis attacks, respectively, through masking the leakage of the clock frequency and supply voltage information in the monitored power profile.

**INDEX TERMS** On-chip voltage regulation, voltage/frequency scaling, security metric, power analysis attacks

# I. INTRODUCTION

Power analysis attacks (PAA) are powerful non-invasive side-channel attacks to obtain the secret key that is stored within cryptographic circuits in feasible time without significant cost [1]–[3]. Differential power analysis (DPA) and leakage power analysis (LPA) attacks are two types of PAA that exploit different characteristics of the side-channel leakage profile [4]–[10]. DPA attacks exploit the correlation between the input data and dynamic power consumption of cryptographic circuits [11]. Alternatively, LPA attacks utilize the correlation between the input data and leakage power dissipation of cryptographic circuits [8].

Dynamic power consumption of a cryptographic circuit is  $P_{dyn} = \alpha f_c V_{dd}^2$  where  $f_c$ ,  $V_{dd}$ , and  $\alpha$  are, respectively, the clock frequency, supply voltage, and activity factor. Activity factor  $\alpha$  is determined by the number of  $0 \rightarrow 1$  transitions that occur in the cryptographic circuit under different input data [12]. To hide the actual dynamic power consumption  $P_{dyn}$  of a cryptographic circuit, different logic families are proposed to make the dynamic power consumption constant under different input data values. The wave dynamic differential logic (WDDL), which is a type of balanced logic gate, is proposed in [13], [14] to make the activity factor  $\alpha$ 

constant regardless of the input data values. A switchedcapacitor current equalizer-based countermeasure is proposed in [15] to achieve a constant  $P_{dyn}$  through discharging the residual charge in every switching cycle. However, DPA attacks countermeasures that hide the dynamic power dissipation of a cryptographic circuit by maintaining constant dynamic power consumption typically cause significant power/area/performance overhead [15], [16]. Alternatively, masking technique [17], [18] is an effective DPA attacks countermeasure that uses random intermediate data values to be inserted among the actual side channel leakage data to reduce the correlation between the input data and  $\alpha$ . However, masking technique may also induce significant area overhead due to the large look-up table (LUT) when a large amount of random data is inserted [17], [18]. Please note that the effectiveness of masking-based countermeasures is directly correlated with the number of inserted data values. There is therefore a tradeoff between the LUT size and the effectiveness of the masking operation.

To minimize the information leakage through the power consumption profile, existing power management techniques that scale voltage and/or frequency at runtime have been tailored as a countermeasure against DPA attacks [4], [5], [11].

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FIGURE 1. Relationship between the clock pulse and power consumption of a cryptographic circuit [5].

These voltage/frequency scaling (VFS) based countermeasures typically randomize the supply voltage and/or the frequency to break the one-to-one relationship between these parameters and the actual workload. Random dynamic voltage and frequency scaling (RDVFS) technique is one of the first VFS-based countermeasures against DPA attacks that reduces the power consumption while also increasing the security [4]. The working principle of the RDVFS technique is to randomly vary  $f_c$  and  $V_{dd}$  to mask the dynamic power variations from an attacker. RDVFS technique, however, has major security flaws since the clock frequency  $f_c$  can be leaked in the input power profile, as demonstrated in Figure 1 [5]. In other words, in a cryptographic circuit that utilizes conventional RDVFS,  $f_c$ becomes a linear function of  $V_{dd}$ , ( $f_c = K_1.V_{dd} + B$  where K and B are the linear parameters) [5].

An attacker can therefore unriddle the fluctuations in the  $f_c$ and  $V_{dd}$  by solely monitoring the width of the spikes in the power consumption profile. After analyzing the pulse width of the monitored power consumption of the cryptographic circuit concurrently with the input data, a cryptographic circuit that houses the RDVFS technique can therefore be breached with negligible effort [5]. Another VFS-based countermeasure, random dynamic voltage scaling (RDVS) technique, is proposed in [5] to disrupt the linear relationship between  $f_c$ and  $V_{dd}$ . Unfortunately, this technique introduces significant power overhead to disrupt the relationship between  $f_c$  and  $V_{dd}$ where the security increases with higher power overhead. In order to minimize the power overhead while utilizing VFS as a countermeasure to secure a cryptographic circuit, Avirneni et al. [11] proposed the aggressive voltage and frequency scaling (AVFS) technique. In the AVFS technique,  $f_c$  and  $V_{dd}$ are independent so that an attacker can no longer estimate the changes in  $V_{dd}$  by solely monitoring the pulse width of the spikes in the monitored power dissipation profile. AVFS technique, however, increases the total chip area by about 3 percent due to redundant register duplication to minimize the circuit contamination delay [11].

Leakage power dissipation primarily has two components: subthreshold power leakage and gate-oxide power leakage [19]. These two power leakage components increase significantly with the continuous scaling of the silicon technology and the reduced supply voltage levels. Conventional LPA attacks are quite sensitive to measurement noise [20] and therefore have attracted relatively less attention as compared to DPA attacks. LPA attacks can still be quite effective if the clock frequency of the cryptographic circuit is lowered by the attacker and the analysis is reinforced with average sampling analysis [21]. Although there are no VFS-based countermeasures specifically tailored against LPA attacks, the leakage power dissipation is naturally affected by the voltage scaling techniques and the aforementioned VFS-based countermeasures are also partly effective against LPA attacks. Moreover, on-chip voltage regulation is becoming an essential part of cryptographic circuits, enabling faster and more power efficient voltage/ frequency scaling (VFS) [22] with less than 1 percent area overhead [23]. In this paper, we investigate the security implications of three different on-chip voltage regulator topologies: low-dropout (LDO) regulator, buck converter, and switchedcapacitor (SC) converter that can be implemented with countermeasures such as RDVFS, RDVS, and AVFS against both DPA and LPA attacks.

The rest of the paper is organized as follows. Security implications of the side-channel leakage mechanisms of three different on-chip voltage regulator topologies (LDO regulator, buck converter, and SC converter) are investigated in Section II. Security evaluations of on-chip voltage regulation with VFS technique against DPA and LPA attacks are provided, respectively, in Sections III and IV. The overhead of a cryptographic circuit that employs different techniques is discussed in Section V. Power attacks simulation is performed in Section VI, while conclusions are offered in Section VII.

## **II. ON-CHIP VOLTAGE REGULATION WITH VFS LOAD**

Each voltage regulator topology has different input and output voltage/current characteristics. These differences change the way how different voltage regulators may leak critical information. In this section, the side-channel leakage mechanisms of three widely used on-chip voltage regulator topologies are investigated.

### A. LOW-DROPOUT (LDO) REGULATOR WITH VFS LOAD

The relationship between the input current  $I_{in}$  and the load current  $I_{load}$  of an LDO regulator, as shown in Figure 2, is

$$I_{in} = I_R + I_{cap} + I_{load}, \tag{1}$$

where  $I_R$  and  $I_{cap}$  are, respectively, the resistor and capacitor current. To minimize the power conversion loss, the resistances of  $R_1$  and  $R_2$  are typically quite large, making the resistor current  $I_R$  negligible. Recently, output-capacitorless LDO voltage regulators have proliferated to reduce the area of LDO regulators [24], [25]. As a result, the capacitor current  $I_{cap}$  can also be ignored in our derivations without loss of generality. The relationship between  $I_{in}$  and  $I_{load}$  can therefore be approximated as



FIGURE 2. Schematic of a conventional LDO voltage regulator.

$$I_{in} \approx I_{load}.$$
 (2)

Similarly, the relationship between the input power  $P_{in}$  and load current  $I_{load}$  can be denoted as

$$P_{in} \approx V_{in} I_{load},$$
 (3)

where  $V_{in}$  is the input voltage. Since there is an approximated linear relationship between  $P_{in}$  and  $I_{load}$ , certain characteristics of the clock frequency  $f_c$  can be estimated by an attacker by monitoring the input power profile.

The relationship between the load current and input power of an LDO voltage regulator is analyzed under a switching load where the clock frequency and supply voltage ( $f_c$ ,  $V_{dd}$ ) pair varies between (440 MHz, 0.8 V) and (830 MHz, 1.2 V) [11]. As shown in Figures 3(a) and 3(b), a linear relationship exists between the load current  $I_{load}$  and input power  $P_{in}$  of an LDO



FIGURE 3. (a) Transient load current profile of an LDO voltage regulator with VFS load. (b) Transient input power profile of an LDO voltage regulator with VFS load.



FIGURE 4. Schematic of a conventional buck converter.

regulator. An attacker can therefore determine the variations in  $f_c$  by monitoring the variations in  $P_{in}$  to nullify RDVFS technique under DPA attacks. The correlation between the input power and load current of an LDO regulator is so high that an attacker can visually extract the workload information without using any advanced analysis techniques.

#### B. BUCK CONVERTER WITH VFS LOAD

A buck converter, as shown in Figure 4, can have three different operating modes: continuous conduction mode (CCM), discontinuous conduction mode (DCM), and the boundary between CCM and DCM, (BCM). The relationships between the input voltage  $V_{in}$  and the output voltage  $V_{dd}$  of a buck converter (shown in Figure 4) operating in these three operating modes are

$$V_{dd} = \begin{cases} DV_{in}, & K_2 > 1 - D, (CCM) \\ DV_{in}, & K_2 = 1 - D, (BCM) \\ \frac{2V_{in}}{1 + \sqrt{1 + 4K_2/D^2}}, & K_2 < 1 - D, (DCM) \end{cases},$$
(4)

where *D* is the duty cycle of the input switching signal. The critical value is  $K_2 = 2Lf_s/R$  where *L* is the inductance of the filter inductor,  $f_s$  is the switching frequency, and *R* is the impedance of load. It is quite difficult for an attacker to analyze the variations of  $V_{dd}$  if the buck converter works in the DCM since the critical value  $K_2$  would become uncertain due to the variations in the value of the load impedance *R* under different input data. An attacker can, however, still determine the changes in  $V_{dd}$  by monitoring the slope of the input power profile which is a strong function of the filter inductor current. When the inductor is in the charging state, the relationship between  $V_{dd}$  and the slope of input current  $S_1$  is

$$S_1 = \frac{dI_{in}}{dt} = \frac{V_{in} - V_{dd}}{L}.$$
(5)

Similarly, the relationship between  $V_{dd}$  and the slope of input power  $S_2$  is

$$S_2 = \frac{dP_{in}}{dt} = \frac{1}{L} (V_{in}^2 - V_{in}V_{dd}).$$
(6)

We investigate the possible leakage of critical workload information through the slope of the monitored input power signature via simulations. The relationship between  $S_2$  and  $V_{dd}$  of a buck converter is analyzed under a switching load when the clock frequency and supply voltage ( $f_c$ ,  $V_{dd}$ ) pair for the switching load varies between (440 MHz, 0.8 V) and (830 MHz, 1.2 V). The switching frequency of buck



FIGURE 5. (a) Transient supply voltage (output voltage)  $V_{dd}$  of a buck converter with VFS load. (b) Transient input power profile of a buck converter with VFS load.

converter is typically around 100 MHz [26]. When  $V_{dd}$  drops from 1.1 to 0.9 V,  $S_2$  increases from 1.78 to 2.27 mW/ns, as shown in Figure 5. An inversely linear relationship exists between  $S_2$  and  $V_{dd}$ , as illustrated in Figure 6. This inversely linear relationship demonstrates the possible information leakage through the slope of input power profile that may nullify RDVFS technique under DPA attacks.

# C. SWITCHED-CAPACITOR (SC) CONVERTER WITH VFS LOAD



An SC voltage converter utilizes one or multiple flying capacitors with a switch network where the flying capacitors

FIGURE 6. Relationship between the supply voltage  $V_{dd}$  and the slope of the input power  $S_2$  in the charging state.

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FIGURE 7. Basic architecture of a switched-capacitor (SC) voltage converter.

charge from the input voltage  $V_{in}$  and discharge to the output node periodically to generate a DC output voltage  $V_{dd}$ . The basic architecture of an SC voltage converter is illustrated in Figure 7. Different voltage conversion ratios can be obtained by modifying the connections of the switches and capacitors within an SC converter.

The relationship between the switching frequency  $f_s$  and the load current  $I_{load}$  of an SC converter is [27]

$$A(V_{dd})f_s = I_{load},\tag{7}$$

where  $A(V_{dd})$  is a function of the supply voltage  $V_{dd}$ . Typically, the switching frequency of an SC converter is around 100 MHz [22], which is much lower than the clock frequency  $f_c$  of a typical S-box which can be around 500 MHz [11]. Therefore, in a single switching period of an SC converter, several spikes occur due to the high clock frequency of the transistors. Assuming that the number of the transitions of load power within a switching period is M, the relationship between  $f_s$  and  $f_c$  can be written as

$$f_{s} = \frac{1}{A(V_{dd})} I_{load} = \frac{1}{A(V_{dd})} \frac{P_{dyn}}{V_{dd}} = \frac{1}{A(V_{dd})} \frac{\sum_{i=1}^{M} \alpha_{i} f_{c} V_{dd}^{2}}{V_{dd}} = \frac{f_{c} V_{dd}}{A(V_{dd})} \sum_{i=1}^{M} \alpha_{i},$$
(8)

where  $P_{dyn}$  is the dynamic power consumption of a cryptographic circuit and  $\alpha_i (i = 1, 2, ...)$  is the corresponding activity factor. While the value of  $\sum_{i=1}^{M} \alpha_i$  is determined by the input data, the switching frequency  $f_s$ , which may be exploited to obtain critical information about  $f_c$ , is masked by scrambling the monitored activity factor  $\sum_{i=1}^{M} \alpha_i$ . An SC converter with a variable  $\sum_{i=1}^{M} \alpha_i$  is analyzed under a switching load circuit with 670 MHz clock frequency and 1 V supply voltage [11] while  $\sum_{i=1}^{M} \alpha_i$  varies between 50 and 400 pF. As shown in Figure 8, the switching frequency  $f_s$  is successfully changed by varying  $\sum_{i=1}^{M} \alpha_i$  in input power profile with a constant  $f_c$ .

When the SC converter is in the charging state, the equality denoting the charging of the flying capacitor should be satisfied as



FIGURE 8. Transient input power of an SC converter with variable  $\sum_{i=1}^{M} \alpha_i$ .

$$\frac{V_{in} - V_1(t)}{R(V_{dd})} = C_{top}(V_{dd}) \frac{dV_1(t)}{dt},$$
(9)

where  $C_{top}(V_{dd})$  is the capacitance of the top plate in the equivalent flying capacitor,  $R(V_{dd})$  is the equivalent series resistance, and  $V_1(t)$  is the voltage of the top plate of the equivalent flying capacitor. The expression for  $V_1(t)$ , the input power in charging state  $P_{in}(t)$ , and the slope of input power in charging state  $S_3$ , respectively, are

$$V_1(t) = V_1(0) + (V_{in} - V_1(0))(1 - e^{-t/R(V_{dd})C_{top}(V_{dd})}),$$
(10)

$$P_{in}(t) = V_{in} \frac{dV_1(t)}{dt} = \frac{V_{in}^2 - V_{in}V_1(0)}{R(V_{dd})C_{top}(V_{dd})} e^{-t/R(V_{dd})C_{top}(V_{dd})},$$
(11)

$$S_3 = \frac{dP_{in}(t)}{dt} = -\frac{V_{in}^2 - V_{in}V_1(0)}{R^2(V_{dd})C_{top}^2(V_{dd})}e^{-t/R(V_{dd})C_{top}(V_{dd})}, \quad (12)$$

where  $V_1(0)$  is the voltage of the top plate in the equivalent flying capacitor before charging. To prevent the leakage of the supply voltage  $V_{dd}$  information through the input power profile from the slope of the input power  $S_3$  in the charging state, the variations of the supply voltage (reflected by  $R(V_{dd})C_{top}(V_{dd})$ ) and the the variations of load power induced by different input data (reflected by  $V_1(0)$ ) are also scrambled together. As shown in Figure 8,  $S_3$  also depends on the variation of  $\sum_{i=1}^{M} \alpha_i$  in input power profile when  $V_{dd}$ is fixed.

# III. SECURITY EVALUATION OF ON-CHIP VOLTAGE REGULATION WITH VFS TECHNIQUE AGAINST DPA ATTACKS

Countermeasures against side-channel attacks either insert noise to the side-channel leakage or reduce the critical signal in the side-channel leakage. VFS-based countermeasures typically insert noise to the power consumption profile to increase the number of measurements that an attacker needs to perform for a successful attack. As mentioned in the *Intro-duction*, the dynamic power consumption of cryptographic circuits  $P_{dyn}$  is

$$P_{dyn} = \alpha f_c V_{dd}^2. \tag{13}$$

After taking logarithm of both of the sides, (13) can be written as

$$log(P_{dyn}) = log(\alpha) + log(f_c) + 2log(V_{dd}), \qquad (14)$$

where  $log(\alpha)$  represents the side-channel signal related with DPA attacks. The amount of uncertain noise  $N_{ik}(f_c, V_{dd})$  that is inserted through different countermeasures that employ three different types of voltage regulators varies significantly, as shown in Table 1. When a cryptographic circuit employs the AVFS technique with an SC converter, the inserted noise would contain both random  $f_c$  and random  $V_{dd}$  due to the independent relationship between  $f_c$  and  $V_{dd}$ . When a cryptographic circuit employs the RDVS technique with an SC converter, the inserted noise would only contain random  $V_{dd}$  as the clock frequency  $f_c$  is fixed. The inserted noise would be zero when the RDVFS technique employs an LDO regulator or a buck converter as either  $f_c$  or  $V_{dd}$  would leak through the input power profile. By utilizing the correlation between  $f_c$  and  $V_{dd}$ , the inserted noise in the side-channel through the countermeasures may be eliminated. However, if a cryptographic circuit employs an SC converter with the RDVFS technique, the uncertain noise would contain both the random clock frequency and supply voltage. As compared to the AVFS technique, a linear relationship exists between the clock frequency  $f_c$  and supply voltage  $V_{dd}$  when the RDVFS technique employs an SC converter. The clock frequency can therefore be denoted as a function of the supply voltage (i.e.,  $f_c =$  $F(V_{dd}) = K_1 \cdot V_{dd} + B$  where  $K_1 = 975$  MHz/V and B =-340 MHz when  $V_{dd} \in [0.8 \text{ V}, 1.2 \text{ V}]$  and  $f_c \in [440 \text{ MHz},$ 830 MHz] [11]).

TABLE 1. Inserted Noise  $N_{j,k}(f_c, V_{dd}), (j, k = 1, 2, 3)$  into the Power Consumption Profile of a Cryptographic Circuit Through Countermeasures That Employ Different Voltage Regulators Against DPA Attacks.

Regulator Technique	LDO regulator	Buck converter	SC converter
RDVFS RDVS AVFS	$egin{aligned} &N_{1,1}(f_c,V_{dd})=0\ &N_{2,1}(f_c,V_{dd})=2\mathrm{log}(V_{dd})\ &N_{3,1}(f_c,V_{dd})=2\mathrm{log}(V_{dd}) \end{aligned}$	$ \begin{split} N_{1,2}(f_c, V_{dd}) &= 0 \\ N_{2,2}(f_c, V_{dd}) &= 0 \\ N_{3,2}(f_c, V_{dd}) &= \log(f_c) \end{split} $	$ \begin{split} N_{1,3}(f_c, V_{dd}) &= \log(F(V_{dd})) + 2\log(V_{dd}) \\ N_{2,3}(f_c, V_{dd}) &= 2\log(V_{dd}) \\ N_{3,3}(f_c, V_{dd}) &= \log(f_c) + 2\log(V_{dd}) \end{split} $

# A. SECURITY OF ON-CHIP VOLTAGE REGULATION WITH TRUE RANDOM VFS TECHNIQUE AGAINST DPA ATTACKS

When all of the aforementioned techniques are true random, the clock frequency  $f_c$  and supply voltage  $V_{dd}$  would have uniform distributions. Let's assume that  $V_{DD1}$  and  $V_{DD2}$  are, respectively, the minimum and maximum voltage values that  $V_{dd}$  can operate. Similarly,  $f_1$  and  $f_2$  are, respectively, the minimum and maximum frequency values that  $f_c$  can take. When the number of discrete values that  $V_{dd}$  can take within  $[V_{DD1}, V_{DD2}]$  is N, the resolution of supply voltage  $\Delta V_{dd}$  and *i*th, (i = 1, 2, 3, ..., N) possible value  $V_{dd,i}$  within  $[V_{DD1}, V_{DD2}]$  can be, respectively, denoted as

$$\Delta V_{dd,i} = \frac{V_{DD2} - V_{DD1}}{N - 1},$$
(15)

$$V_{dd,i} = \frac{(i-1) \times (V_{DD2} - V_{DD1})}{N-1} + V_{DD1}.$$
 (16)

Similarly, assuming that frequency can get *N* different values within  $[f_1, f_2]$ , the *i*th possible value  $f_{c,i}$  can be denoted as

$$f_{c,i} = \frac{(i-1) \times (f_2 - f_1)}{N - 1} + f_1.$$
(17)

If the frequency<sup>1</sup> of the voltage scaling operation is  $f_v$ , the mean value of the inserted noise  $E(N_{j,k}(f_c, V_{dd}))$  for on-chip voltage regulation based and uniformly distributed RDVFS technique (j = 1), RDVS technique (j = 2), and AVFS technique (j = 3), respectively, are

$$E(N_{1,k}(f_c, V_{dd})) = \frac{1}{\sum_{i=1}^{N} \left[\frac{f_{c,i}}{f_v}\right]} \sum_{i=1}^{N} \left[\frac{f_{c,i}}{f_v}\right] N_{1,k}(f_{c,i}, V_{dd,i}),$$
(18)

$$E(N_{2,k}(f_c, V_{dd})) = \frac{1}{N} \sum_{i=1}^{N} N_{2,k}(f_c, V_{dd,i}),$$
(19)

$$E(N_{3,k}(f_c, V_{dd})) = \frac{1}{N \sum_{l=1}^{N} \left[\frac{f_{c,l}}{f_v}\right]} \sum_{l=1}^{N} \sum_{i=1}^{N} \left[\frac{f_{c,l}}{f_v}\right] N_{3,k}(f_{c,l}, V_{dd,i}).$$
(20)

The corresponding variance of the inserted noise  $Var(N_{j,k}(f_c, V_{dd}))$  can be denoted, respectively, as

$$Var(N_{1,k}(f_{c}, V_{dd})) = \frac{1}{\sum_{i=1}^{N} \left[\frac{f_{c,i}}{f_{v}}\right]} \sum_{i=1}^{N} \left[\frac{f_{c,i}}{f_{v}}\right] (N_{1,k}(f_{c,i}, V_{dd,i}) - E(N_{1,k}(f_{c}, V_{dd})))^{2},$$
(21)

$$Var(N_{2,k}(f_c, V_{dd})) = \frac{1}{N} \sum_{i=1}^{N} (N_{2,k}(f_c, V_{dd,i}) - E(N_{2,k}(f_c, V_{dd})))^2,$$
(22)

<sup>1</sup>Since on-chip voltage regulator can generate variable supply voltage levels  $V_{dd}$ , we assume that the frequency of the voltage scaling is  $f_{\nu}$ .



FIGURE 9. Relationship between the input data and monitored power consumption  $P_{dyn}$  of a cryptographic circuit that employs an on-chip voltage regulation based VFS technique (*Conventional cryptographic circuit* represents a cryptographic circuit without any countermeasure).

$$Var(N_{3,k}(f_{c}, V_{dd})) = \frac{1}{N \sum_{i=1}^{N} \left[\frac{f_{c,l}}{f_{v}}\right]} \times \sum_{l=1}^{N} \sum_{i=1}^{N} \left[\frac{f_{c,l}}{f_{v}}\right] (N_{3,k}(f_{c,l}, V_{dd,i}) - E(N_{3,k}(f_{c}, V_{dd})))^{2}.$$
(23)

A cryptographic circuit that employs on-chip voltage regulation based VFS technique can be modeled with two separate noise insertion blocks (noise block<sub>1</sub> and noise block<sub>2</sub>), as shown in Figure 9. Accordingly, the correlation coefficient between the input data and monitored power consumption  $P_{dyn}$  of that cryptographic circuit can be represented with the correlation between the input data and monitored power dissipation of those two noise insertion blocks. The signal-to-noise ratio (SNR) at the output of the noise block<sub>2</sub>  $SNR''_{ik}$  can be denoted as

$$SNR''_{j,k} = \frac{Var(log(\alpha))}{Var(N_{j,k}(f_c, V_{dd}))},$$
(24)

where  $Var(log(\alpha))$  represents the variance of  $log(\alpha)$ . The correlation coefficient  $\gamma''_{j,k}$  between the activity factor  $\alpha$  and monitored power dissipation  $P_{dyn}$  of the cryptographic circuit can be obtained as [12]

$$\gamma_{j,k}'' = \frac{1}{\sqrt{1 + \frac{1}{SNR_{j,k}''}}}.$$
(25)

Correlation coefficient between the input data and monitored power dissipation of the cryptographic circuit is widely used as a metric to evaluate the level of security [8], [12], [29]. Since the operations that take place in the noise block<sub>1</sub> are independent of the operations that take place in the noise block<sub>2</sub>, the correlation coefficient  $\gamma_{j,k}$  between the input data and monitored power consumption can be written as [12]

$$\gamma_{j,k} = \gamma' \times \gamma_{j,k}'' \tag{26}$$

where  $\gamma'$  is the correlation coefficient between the input data and activity factor. Therefore,  $(1 - \gamma''_{j,k})$  can be defined as the *correlation coefficient reduction ratio* of a cryptographic



FIGURE 10. Variance of supply voltage  $V_{dd}$  versus the correlation coefficient reduction ratio of an-S-box that employs different VFS-based countermeasures (VFS techniques conform to uniform distribution and N = 50. Since a high  $f_v$  does not enhance the variance of noise induced by VFS technique, as explained in [5], [11], a moderate voltage scaling frequency of  $f_v = 10$  MHz [28] is used for the security analysis to not increase the system design complexity).

circuit that employs a VFS-based countermeasure with onchip voltage regulation.

A low power and small area substitution-box (S-box) from [30] is implemented at the 130nm CMOS technology node and utilized as the cryptographic circuit under attack. The correlation coefficient reduction ratio that is achieved when different countermeasures are employed to protect the S-box is shown in Figure 10. The S-box that employs an SC converter based RDVFS technique exhibits the highest correlation coefficient reduction ratio under the same variance of  $V_{dd}$ . The security implications of the number of  $(f_c, V_{dd})$  pairs N are investigated. As shown Figure 11, the number of possible  $(f_c, V_{dd})$  pairs N has a negligible impact on the correlation coefficient reduction ratio of an S-box that employs RDVFS technique with an SC converter. Additionally, when the variance of  $V_{dd}$  exceeds 0.04 $V^2$ , the correlation coefficient reduction ratio of an S-box that employs RDVFS technique with an SC converter starts converging, as shown in Figure 10. A higher variance of  $V_{dd}$  causes increased performance degradation for a cryptographic circuit that employs RDVFS technique [11]. Selecting the variance of  $V_{dd}$  as 0.04 V<sup>2</sup>, therefore, provides a reasonable design tradeoff between security and performance. When the variance of  $V_{dd}$  is equal to  $0.04V^2$ , an S-box that employs RDVFS technique with an SC converter performs best against DPA attacks as compared to an S-box employs other techniques without significant performance degradation.

Since a true random VFS technique may be difficult to implement in practice, a statistically normally distributed VFS technique is used in the modern processors [31]–[33].



FIGURE 11. Variance of the supply voltage  $V_{dd}$  versus the correlation coefficient reduction ratio for an S-box that employs RDVFS technique with an SC converter with various possible  $(f_c, V_{dd})$  pairs.

The detail security analysis of on-chip voltage regulation with normally distributed VFS technique against DPA attacks can be found in Appendix C.

# IV. SECURITY EVALUATION OF ON-CHIP VOLTAGE REGULATION WITH VFS TECHNIQUE AGAINST LPA ATTACKS

A leakage power analysis (LPA) attack is a type of side-channel attack, which is utilized by an attacker to leak the secret key by exploiting the correlation between the input data and leakage power dissipation of a cryptographic circuit [8]. The side-channel leakage current of a cryptographic circuit  $I_{leak}$ can be denoted as [8]

$$I_{leak} = \omega I_H + (m - \omega) I_L, \qquad (27)$$

where  $\omega$  is the hamming weight of input data and *m* is the number of bits in the input data.  $I_H(I_L)$  is the leakage current when the input bit is high (low). Since  $I_H(I_L)$  is a function of the supply voltage  $V_{dd}$  [34], the leakage power dissipation  $P_{leak}$  of a cryptographic circuit can be written as

$$P_{leak} = V_{dd}I_{leak}$$
  
=  $V_{dd}(\omega I_H(V_{dd}) + (m - \omega)I_L(V_{dd}))$  (28)  
=  $V_{dd}I_{leak,0}K(V_{dd}),$ 

where  $I_{leak,0}$  is the component of leakage current which is independent of the supply voltage  $V_{dd}$  and  $K(V_{dd})$  is the component of leakage current which is strongly correlated with  $V_{dd}$ .

In sub-micro CMOS integrated circuits (ICs), the relationship between the leakage current of the CMOS ICs and supply voltage  $V_{dd}$  can be approximated as an exponent relationship ( $I_{leak} = I_{leak,0}K(V_{dd}) \approx I_{leak,0}exp(aV_{dd})$ ) [34]. In order to determine the value of the parameter *a*, two different



FIGURE 12. Supply voltage  $V_{dd}$  versus leakage current of an S-box implemented in 130 nm CMOS technology under two different input data.

input data patterns (input data<sub>1</sub> and input data<sub>2</sub>) are applied to a 130 nm CMOS based S-box [30]. The simulated relationship between the leakage current and supply voltage  $V_{dd}$  is shown in Figure 12. We use two different exponent functions  $K_1(V_{dd}) = b_1 exp(aV_{dd})$  and  $K_2(V_{dd}) = b_2 exp(aV_{dd})$  to curvefit the relationship between the leakage current and supply voltage  $V_{dd}$  induced by input data<sub>1</sub> and input data<sub>2</sub>, respectively. After fitting as shown in Figure 12, the expressions of  $K_1(V_{dd})$  and  $K_2(V_{dd})$  can be respectively determined as

$$K_1(V_{dd}) = 27 \times exp(1.19 \times V_{dd}) \approx 27K(V_{dd}), \qquad (29)$$

$$K_2(V_{dd}) = 28.29 \times exp(1.19 \times V_{dd}) \approx 28.29 K(V_{dd}).$$
 (30)

Therefore, the leakage power dissipation of the S-box  $P_{leak}$  can be denoted as

$$P_{leak} = V_{dd} I_{leak,0} K(V_{dd}),$$

$$\approx V_{dd} \times I_{leak,0} \times exp(1.19 \times V_{dd}).$$
(31)

After taking logarithm of both sides, (31) becomes

$$log(P_{leak}) \approx log(I_{leak,0}) + log(V_{dd}) + 1.19V_{dd}, \qquad (32)$$

where  $log(I_{leak,0})$  is the side-channel signal which may provide useful information under an LPA attack. The characteristics of



FIGURE 13. Variance of supply voltage  $V_{dd}$  versus the correlation coefficient reduction ratio of an S-box that employs different countermeasures ( $f_v = 10 \text{ MHz}$ , and N = 50).

the inserted noise  $M_{j,k}(V_{dd})$  to an S-box through different countermeasures against LPA attacks are listed in Table 2. Since a buck converter leaks the supply voltage  $V_{dd}$  from the slope of input power, the uncertain noise  $M_{j,2}(V_{dd})$  that is inserted by a buck converter based VFS technique becomes zero.

As shown in Figure 13, an S-box that employs the RDVFS technique with an SC converter can achieve a correlation coefficient reduction ratio of over 90 percent when the variance of supply voltage  $V_{dd}$  is greater than 0.04 V<sup>2</sup>.

#### V. OVERHEAD ANALYSIS

The power overhead of several VFS-based countermeasures with on-chip voltage regulation is summarized in Table 3. An S-box [30] that houses an SC voltage converter exhibits the highest correlation coefficient reduction ratio (CCRR) of about 85.41 percent (80.94 percent) with true random (normally distributed) RDVFS technique under DPA attacks and about 94.3 percent (92.41 percent) with true random (normally distributed) RDVFS technique under LPA attacks. The corresponding dynamic power (D-Power) consumption of the S-box is  $0.746X_d$  ( $0.692X_d$ ) with true random (normally distributed) RDVFS technique whereas the corresponding leakage power (L-Power) dissipation is  $0.7116X_l$  ( $0.6948X_l$ ) with true random (normally distributed) RDVFS technique.

TABLE 2. Inserted Noise  $M_{j,k}(V_{dd}), (j, k = 1, 2, 3)$  into the Power Consumption Profile of a Cryptographic Circuit Through Countermeasures That Employ Different Voltage Regulators Against LPA Attacks.

Regulator	LDO regulator	Buck converter	SC converter
Technique			
RDVFS RDVS	$M_{1,1}(V_{dd}) = \log(V_{dd}) + 1.19V_{dd}$ $M_{2,1}(V_{dd}) = \log(V_{dd}) + 1.19V_{dd}$	$M_{1,2}(V_{dd}) = 0$ $M_{2,2}(V_{dd}) = 0$	$M_{1,3}(V_{dd}) = \log(V_{dd}) + 1.19V_{dd}$ $M_{2,3}(V_{dd}) = \log(V_{dd}) + 1.19V_{dd}$
AVFS	$M_{3,1}^{2,1}(V_{dd}) = \log(V_{dd}) + 1.19V_{dd}$	$M_{3,2}^{2,2}(V_{dd}) = 0$	$M_{3,3}(V_{dd}) = \log(V_{dd}) + 1.19V_{dd}$

TABLE 3. Correlation Coefficient Reduction Ratio (CCRR), Dynamic Power (D-Power) Consumption, and Leakage Power (L-Power) Consumption of an S-Box That Houses On-Chip Voltage Regulators Implemented with True Random and Normally Distributed VFS-based Countermeasures Against DPA and LPA Attacks (Supply Voltage Range  $V_{DD2} - V_{DD1} = 0.7V$ ).  $X_d$  and  $X_l$  are, Respectively, the Dynamic and Leakage Power Consumption of an S-box Without Any Countermeasure.

	DPA attacks			LPA attacks				
	True random		Normally distributed		True random		Normally distributed	
	CCRR	D-Power	CCRR	D-Power	CCRR	L-Power	CCRR	L-Power
LDO+RDVFS	0	$0.746X_d$	0	$0.692X_d$	94.3%	$0.7116X_l$	92.41%	$0.6948X_l$
Buck+RDVFS	0	$0.746X_d$	0	$0.692X_d$	0	$0.7116X_l$	0	$0.6948X_l$
SC+RDVFS	85.41%	$0.746X_d$	80.94%	$0.692X_d$	94.3%	$0.7116X_l$	92.41%	$0.6948X_l$
LDO+RDVS	61.2%	$2.0391X_d$	51.07%	$2.0195X_d$	92.56%	$2.7274X_l$	90.14%	$2.6820X_l$
Buck+RDVS	0	$2.0391X_d$	0	$2.0195X_d$	0	$2.7274X_l$	0	$2.6820X_l$
SC+RDVS	61.2%	$2.0391X_d$	51.07%	$2.0195X_d$	92.56%	$2.7274X_l$	90.14%	$2.6820X_l$
LDO+AVFS	76.43%	$0.6097X_d$	69.07%	$0.5427X_d$	94.3%	$0.7116X_l$	92.41%	$0.6948X_l$
Buck+AVFS	68.32%	$0.6097X_d$	59.52%	$0.5427X_d$	0	$0.7116X_l$	0	$0.6948X_l$
SC+AVFS	80.74%	$0.6097X_d$	77.31%	$0.5427X_d$	94.3%	$0.7116X_l$	92.41%	$0.6948X_l$

 $X_d$  represents the dynamic power consumption of an S-box without any countermeasure and  $X_l$  is the leakage power dissipation of an S-box without any countermeasure. A detailed explanation of power consumption overhead of different techniques tabulated in Table 3 can be found in Appendix B.

There are two main sources of the additional area overhead that need to be considered for an S-box that employs a VFS technique with an on-chip voltage regulator: area overhead induced by on-chip voltage regulator and area overhead induced by VFS technique. Since an on-chip voltage regulator utilized to generate fast VFS [22] causes less than 1 percent area overhead [23], the area overhead induced by on-chip voltage regulator can be neglected. The VFS techniques, RDVFS and RDVS, would not cause extra area overhead based on the analysis provided in [5], [11]. AVFS technique, however, has a 3 percent area overhead induced by the redundant register duplication to minimize the circuit contamination delay [11].

## **VI. DPA AND LPA ATTACK SIMULATIONS**

DPA and LPA attacks are performed in Cadence on two different S-boxes that are implemented at 130 nm CMOS technology: one S-box [30] without any countermeasure and another S-box [30] that employs a true random RDVFS technique with an SC converter. As shown in Figure 14, the correct key<sup>2</sup> of the S-box without countermeasure can be obtained by performing DPA attacks or LPA attacks after inputting 1,000 plaintexts. However, the correlation coefficient of the correct key under LPA attacks is higher than the correlation coefficient of the correct key under DPA attacks. This can be interpreted as LPA attacks are able to leak a higher amount of critical information from the S-box as compared to DPA attacks when there is no countermeasure.

<sup>&</sup>lt;sup>2</sup>In hamming-weight model, the correlation coefficient distinction between the correct key and complement of the correct key is the polarity [8]. The correlation coefficient of the correct key is positive, while the correlation coefficient of the complement of the correct key is negative. In order to make the highest correlation coefficient more obvious, in Figures 14 and 15, we normalized all of the correlation coefficients with absolute values.



FIGURE 14. Absolute value of the correlation coefficient versus all of the possible keys after inputting 1,000 plaintexts with the hamming-weight model. (a) An S-box without countermeasure under DPA attacks. (b) An S-box without countermeasure under LPA attacks.



FIGURE 15. Absolute value of correlation coefficient versus all the possible keys after inputting 1 million plaintexts with hamming-weight model ( $V_{DD2} - V_{DD1} = 0.7V$ ). (a) An S-box that employs RDVFS technique with an SC converter under DPA attacks. (b) An S-box that employs RDVFS technique with an SC converter under LPA attacks.

In the second experiment, DPA and LPA attacks are performed against an S-box that employs a true random RDVFS technique with an SC converter. After inputting one million plaintexts, neither DPA nor LPA attacks are able to fetch the correct key as shown in Figure 15. However, the correlation coefficient of the correct key under LPA attacks is much lower than the correlation coefficient of the correct key under DPA attacks when RDVFS technique with an SC converter is enabled. This behavior indicates that LPA attacks are more sensitive to noise.

After inputting one million plaintexts to the S-box that employs a true random RDVFS technique with an SC converter, the correlation coefficient reduction ratio of the correct key is 88.53 percent (97.77 percent) under DPA (LPA) attacks. These values are higher than the theoretical values of 85.41 percent (94.3 percent) which are listed in Table 3. An intuitive explanation is provided below. • The theoretical values tabulated in Table 3 are the correlation coefficient reduction ratios of an S-box that employs different countermeasures assuming that the attacker can apply any number of attacks until the secret key within the S-box is obtained (i.e., more than one million plaintexts). However, in DPA and LPA attack simulations, we applied one million plaintexts and the S-box that employs a true random RDVFS technique with an SC converter could not be cracked after inputting one million plaintexts as shown in Figure 15. This indicates the presence of significant amount of noise in the S-box. If more plaintexts are applied to filter the noise, the correlation coefficient of the correct key would be enhanced and the correlation coefficient reduction ratio would decrease, approaching the theoretical value.

#### **VII. CONCLUSION**

The security implications of different on-chip voltage regulator topologies implemented within various voltage/ frequency scaling-based countermeasures such as RDVFS, RDVS, and AVFS techniques against power analysis attacks are investigated. The side-channel leakage mechanisms of three widely used on-chip voltage regulator topologies are investigated. The security impact of on-chip voltage regulators is evaluated based on the correlation coefficient between the input data and monitored power consumption of a cryptographic circuit. Correlation coefficient reduction ratio is proposed to simplify the security evaluation. RDVFS technique implemented with a switched-capacitor voltage converter can reduce correlation coefficient over 80 percent (92 percent) against DPA (LPA) attacks and the measurement-to-disclose (MTD) value is enhanced over 1 million by masking the clock frequency, supply voltage, and dynamic power consumption information from a malicious attacker.

# **APPENDIX A**

#### **DETAILED EXPLANATION OF TABLES 1 AND 2**

As demonstrated in Section II, the parameters that leak due to the usage of three different voltage regulators with a VFS load can be summarized in Table 4 a. As explained in Section II, an LDO regulator leaks the information regarding the clock frequency  $f_c$  of the VFS load, while a buck converter leaks information regarding the supply voltage  $V_{dd}$  of the VFS load. However, an SC converter with VFS load prevents the leakage of  $f_c$  and  $V_{dd}$  as demonstrated in Section II-C.

The inserted noise induced by three different VFS techniques against DPA attacks is shown in Table 4 b. For RDVFS technique against DPA attacks, the inserted noise can be written as  $log(f_c) + 2log(V_{dd})$  based on Equation (14). Since, there is a one-to-one linear relationship between  $f_c$  and  $V_{dd}$  in RDVFS technique, the relationship between  $f_c$  and  $V_{dd}$  can be denoted as  $f_c = F(V_{dd})$  or  $V_{dd} = F^{-1}(f_c)$  where  $F^{-1}$  is the inverse function of F. Therefore, the inserted noise induced by RDVFS technique against DPA attacks also can be TABLE 4. (a) Parameter Leakage of Three Different Voltage Regulators with VFS Load. (b) Inserted Noise Induced by Three Different VFS Techniques Against DPA Attacks. (c) Inserted Noise Induced by Three Different VFS Techniques Against LPA Attacks.

	(a)					
	LDO regulator	Buck Converter	SC converter			
Leakage	$f_c$	$V_{dd}$	0			
		(b)				
	RDVFS	RDVS	AVFS			
Noise	$\log(F(V_{dd})) + 2\log(V_{dd})$	$2\log(V_{dd})$	$\log(f_c) + 2\log(V_{dd})$			
	or					
	$\log(f_c) + 2\log(F^-(f_c))$					
		(c)				
	RDVFS	RDVS	AVFS			
Noise	$\log(V_{dd}) + 1.19V_{dd}$	$\log(V_{dd}) + 1.19V_{dd}$	$\log(V_{dd}) + 1.19V_{dd}$			

written as  $log(F(V_{dd})) + 2log(V_{dd})$  or  $log(f_c) + 2log(F^{-1}(f_c))$ . For RDVS technique against DPA attacks, since clock frequency  $f_c$  is fixed, from Equation (14), the inserted noise can be written as  $2log(V_{dd})$ . However, for AVFS technique against DPA attacks, from Equation (14), the inserted noise is  $log(f_c) + 2log(V_{dd})$ . Unlike RDVFS technique, the clock frequency  $f_c$  is independent of the supply voltage  $V_{dd}$  in AVFS technique, therefore,  $f_c$  can not be denoted as a function of  $V_{dd}$  in AVFS technique.

As shown in Table 1, when an LDO regulator is implemented within different VFS techniques against DPA attacks, the VFS noise related to  $f_c$  can be eliminated due to the leakage of  $f_c$ . Similarly, for a buck converter implemented within different VFS techniques against DPA attacks, the VFS noise related to  $V_{dd}$  can be eliminated due to the leakage of  $V_{dd}$ . Since an SC converter implemented within different VFS techniques against DPA attacks prevents the leakage of  $f_c$  and  $V_{dd}$ , the VFS noise is retained without reduction.

The inserted noise induced by three different VFS techniques against LPA attacks is shown in Table 4 c. Since all of the VFS techniques (RDVFS, RDVS, and AVFS) contain the information of the  $V_{dd}$  scaling as demonstrated in Equation (32), the inserted noise from all of the VFS techniques against LPA attacks can be written as  $log(V_{dd}) + 1.19V_{dd}$ . Since a buck converter with a VFS load leaks the supply voltage  $V_{dd}$ , the inserted noise from a buck converter with different VFS techniques related with  $V_{dd}$  against LPA attacks can be eliminated, as tabulated in Table 2.

#### **APPENDIX B**

# DETAILED ANALYSIS OF POWER CONSUMPTION OVERHEAD OF DIFFERENT COUNTERMEASURES

The dynamic power dissipation  $P_{dyn}$  of the S-box mentioned in the paper is



FIGURE 16. Supply voltage  $V_{dd}$  versus clock frequency  $f_c$  under different VFS techniques. (a) RDVS technique. (b) RDVFS technique. (c) AVFS technique.

$$P_{dyn} = \alpha f_c V_{dd}^2. \tag{33}$$

In Figure 16(a),  $(f'_{c,0}, V'_{dd,0})$  is the clock frequency and supply voltage of an S-box that does not employ a VFS technique. When the S-box employs RDVS technique as shown in Figure 16(a), the supply voltage becomes higher than  $V'_{dd,0}$ , increasing the dynamic power dissipation of the S-box as compared to the dynamic power dissipation of the S-box without a VFS technique.

When an S-box employs RDVFS technique as shown in Figure 16(b), the clock frequency and supply voltage can be lower than  $f'_{c,0}$  and  $V'_{dd,0}$ , respectively. As a result, the dynamic power dissipation of the S-box that employs RDVFS technique is lower than the dynamic power dissipation of the S-box without a VFS technique.

When an S-box employs AVFS technique as shown in Figure 16(c), the clock frequency and supply voltage can also be lower than  $f'_{c,0}$  and  $V'_{dd,0}$ , respectively. However, as compared to RDVFS technique, the clock frequency and supply voltage of an S-box that employs AVFS technique no longer have a one-to-one relationship (i.e., the clock frequency is independent of the supply voltage). Therefore, when the supply voltage is high, the clock frequency does not need to be high in AVFS technique. This property of the AVFS technique can make the dynamic power dissipation of the S-box that employs AVFS technique lower than the dynamic power dissipation of the S-box that employs RDVFS technique.

The leakage power dissipation  $P_{leak}$  of an S-box as derived as

$$P_{leak} \approx V_{dd} \times I_{leak,0} \times exp(1.19 \times V_{dd}).$$
(31a)

Unlike the dynamic power dissipation  $P_{dyn}$  of an S-box, the leakage power dissipation  $P_{leak}$  is actually independent of the clock frequency  $f_c$ .

When an S-box employs RDVS technique as shown in Figure 16(a), since the the supply voltage is higher than  $V'_{dd,0}$ , the leakage power dissipation of the S-box employs RDVS technique is higher than the leakage power dissipation of the S-box that does not employ a VFS technique. For an S-box that employs either RDVFS or AVFS technique (respectively illustrated in Figures 16(b) and 16(c)), since the the supply voltage can be lower than  $V'_{dd,0}$ , the leakage power dissipation of the S-box that employs RDVFS or AVFS technique is lower than the leakage power dissipation of the S-box that employs RDVFS or AVFS technique is lower than the leakage power dissipation of the S-box that employs RDVFS or AVFS technique is lower than the leakage power dissipation of the S-box that does not employ a VFS technique.

# APPENDIX C SECURITY OF ON-CHIP VOLTAGE REGULATION WITH NORMALLY DISTRIBUTED VFS TECHNIQUE AGAINST DPA ATTACKS

Assuming that the clock frequency  $f_c$  and the supply voltage  $V_{dd}$  of a RDVFS technique conform to a normal distribution with the mean values  $\mu_f$  and  $\mu_v$ , respectively, as

$$\mu_f = \frac{f_1 + f_2}{2},\tag{34}$$

$$\mu_{\nu} = \frac{V_{DD1} + V_{DD2}}{2},\tag{35}$$

the relationship between the variance of the clock frequency  $\sigma_f^2$  and the variance of the supply voltage  $\sigma_v^2$  becomes

$$\sigma_f^2 = \left(\frac{\mu_f}{\mu_\nu}\right)^2 \sigma_\nu^2. \tag{36}$$

If  $\Delta V_{dd}$  is the minimum supply voltage resolution that is defined as

$$\Delta V_{dd} = \frac{V_{DD2} - V_{DD1}}{N - 1},$$
(37)

the below approximated equation is satisfied when N is sufficiently large

$$\sum_{i=1}^{N} \frac{\Delta V_{dd}}{\sigma_{v} \sqrt{2\pi}} exp\left(-\frac{\left(V_{dd,i} - \mu_{v}\right)^{2}}{2\sigma_{v}^{2}}\right) \approx 1.$$
(38)

Assuming that the total number of input  $(f_c, V_{dd})$  data is W, the corresponding number of input  $(f_{c,i}, V_{dd,i})$  data  $W_i$  is

$$W_i \approx \frac{W}{\sigma_v \sqrt{2\pi}} exp\left(-\frac{\left(V_{dd,i} - \mu_v\right)^2}{2\sigma_v^2}\right).$$
(39)

The mean value of the uncertain noise  $E(N_{j,k}(f_c, V_{dd}))$  for on-chip voltage regulation based and normally distributed RDVFS technique (j = 1), RDVS technique (j = 2), and AVFS technique (j = 3) become

$$E(N_{1,k}(f_c, V_{dd})) = \frac{1}{\sum_{i=1}^{N} W_i \left[\frac{f_{c,i}}{f_v}\right]} \sum_{i=1}^{N} W_i \left[\frac{f_{c,i}}{f_v}\right] N_{1,k}(f_{c,i}, V_{dd,i}),$$
(40)

$$E(N_{2,k}(f_c, V_{dd})) = \frac{1}{\sum_{i=1}^{N} W_i} \sum_{i=1}^{N} W_i N_{2,k}(f_c, V_{dd,i}), \quad (41)$$

$$E(N_{3,k}(f_c, V_{dd})) = \frac{1}{\sum_{l=1}^{N} \sum_{i=1}^{N} W_l W_l \left[\frac{f_{c,l}}{f_v}\right]} \times \sum_{l=1}^{N} \sum_{i=1}^{N} W_l W_l \left[\frac{f_{c,l}}{f_v}\right] N_{3,k}(f_{c,l}, V_{dd,i}).$$
(42)



FIGURE 17. Variance of supply voltage  $V_{dd}$  versus correlation coefficient reduction ratio of an S-box that employs different techniques (VFS techniques conform to normal distribution,  $f_{\nu} = 10 \text{ MHz}$ , and N = 50) as compared to uniformly distributed RDVFS with an SC voltage converter.

The corresponding variance of uncertain noise  $Var(N_{1,k}(f_c, V_{dd}))$  can be written as

$$Var(N_{1,k}(f_{c}, V_{dd})) = \frac{1}{\sum_{i=1}^{N} W_{i} \left[\frac{f_{c,i}}{f_{v}}\right]}$$

$$\times \sum_{i=1}^{N} W_{i} \left[\frac{f_{c,i}}{f_{v}}\right] (N_{1,k}(f_{c,i}, V_{dd,i}) - E(N_{1,k}(f_{c}, V_{dd})))^{2},$$
(43)

$$Var(N_{2,k}(f_c, V_{dd})) = \frac{1}{\sum_{i=1}^{N} W_i} \times \sum_{i=1}^{N} W_i(N_{2,k}(f_c, V_{dd,i}) - E(N_{2,k}(f_c, V_{dd})))^2,$$
(44)

$$Var(N_{3,k}(f_c, V_{dd})) = \frac{1}{\sum_{l=1}^{N} \sum_{i=1}^{N} W_l W_i \left[\frac{f_{c,l}}{f_v}\right]} \times \sum_{l=1}^{N} \sum_{i=1}^{N} W_l W_i \left[\frac{f_{c,l}}{f_v}\right] (N_{3,k}(f_{c,l}, V_{dd,i}) - E(N_{3,k}(f_c, V_{dd})))^2.$$
(45)

As shown in Figure 17, an S-box [30] with the RDVFS technique employing an SC converter still exhibits the highest correlation coefficient reduction ratio as compared to the S-boxes that employ other techniques. Moreover, as compared to the S-box with uniformly distributed RDVFS technique employing an SC converter, the S-box with normally distributed RDVFS technique employing an SC converter has a slightly lower correlation coefficient reduction ratio under the same variance of the supply voltage. However, as shown in Figure 18, for achieving the same variance of supply voltage, the normally distributed RDVFS technique



FIGURE 18. Variance of the supply voltage  $V_{dd}$  versus the supply voltage range  $(V_{DD2} - V_{DD1})$  for uniformly and normally distributed  $V_{dd}$ .

needs to have a larger supply voltage range  $(V_{DD2} - V_{DD1})$ , which would degrade the performance of the cryptographic circuits as compared to the uniformly distributed RDVFS technique.

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