Quantum Imaging Technologies: Quantum Laser Radar

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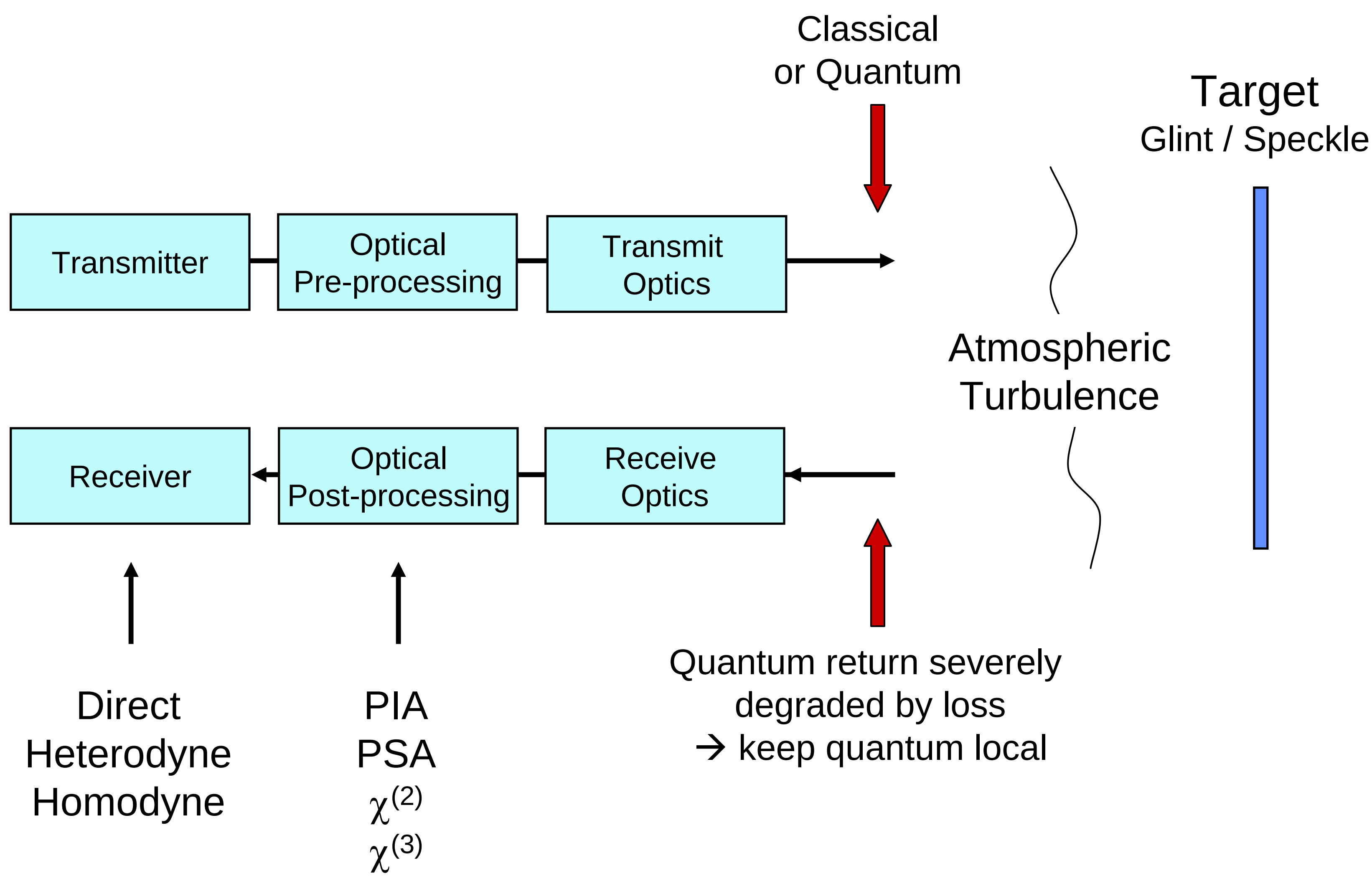
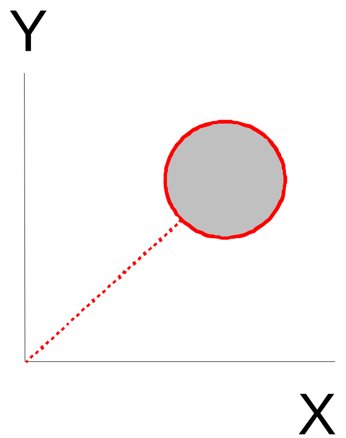
Quantum Laser Radar

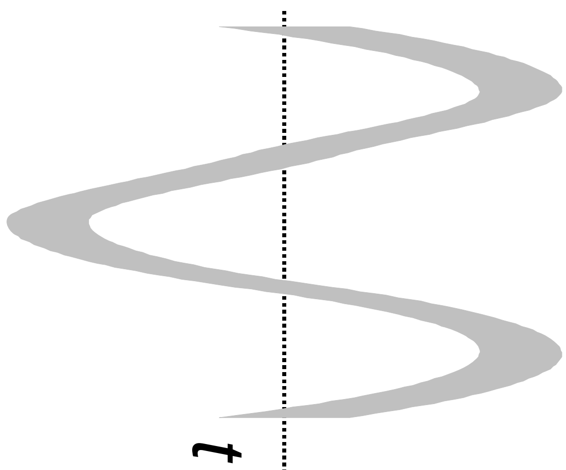


PIA = Phase Insensitive Amplifier
PSA = Phase Sensitive Amplifier

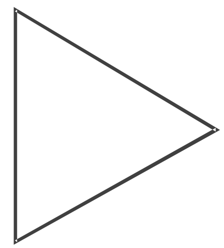
Pictorial View of Amplification of Coherent Input Light

$$E = X + i\,Y$$

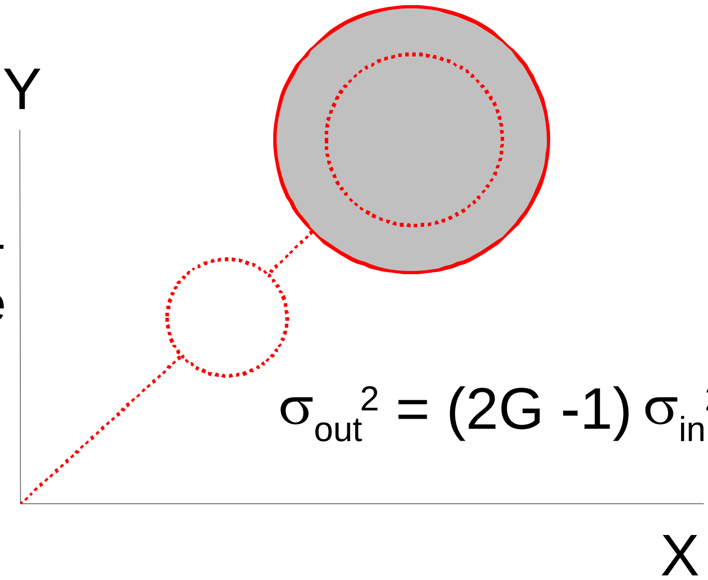




$$\mathcal{E} = X \cos \omega t - Y \sin \omega t$$

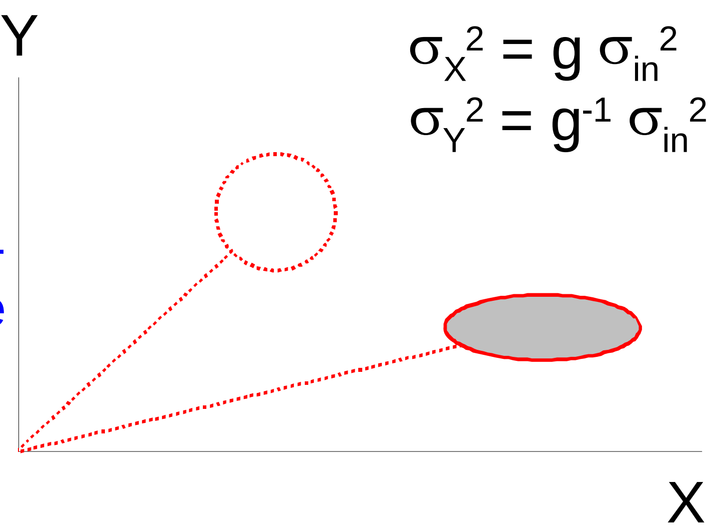


Phase-insensitive



$$\sigma_{out}^2 = (2G - 1)\,\sigma_{in}^2$$

Phase-sensitive



$$\sigma_X^2 = g\,\sigma_{in}^2$$

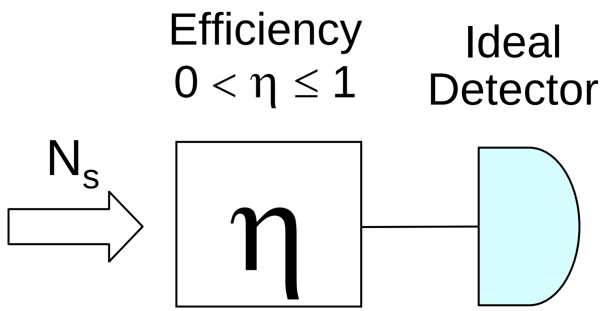
$$\sigma_Y^2 = g^{-1}\,\sigma_{in}^2$$

Simulation of Preamplified Photodetection of Shot-Noise Limited Signals

- Simulation of the amplification of a gray-scale image in the shot-noise limited regime
- Random zero-mean Gaussian noise is added to represent detector noise
  - A valid model when the received signal photon number per pulse or per inverse bandwidth is large
- Photocurrents in the unamplified and amplified cases are scaled appropriately for fair comparison.

Simulation of Preamplified Photodetection of Shot-Noise Limited Signals

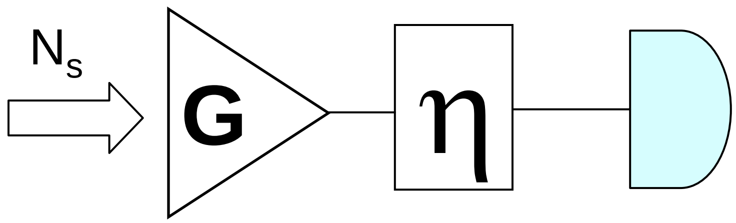
- For $G = 1$ (no preamplification)
  - $SNR_{IN} = N_s$ (shot-noise limited signal)
  - $\langle(\Delta N_s)^2\rangle_\eta = \eta N_s$, $SNR_{OUT} = \eta N_s$
  - $NF = SNR_{IN} / SNR_{OUT} = 1/\eta$



- For $G > 1$
  - $SNR_{IN} = N_s$ and $\langle(\Delta N_s)^2\rangle = N_s$
  - Output = $\eta G N_s$. Find $\langle(\Delta N_s)^2\rangle_{\eta G}$ from:
  - $NF = SNR_{IN} / SNR_{OUT} = N_s / [(\eta G N_s)^2 / \langle(\Delta N_s)^2\rangle_{\eta G}]$

  …or…

  - $\langle(\Delta N_s)^2\rangle_{\eta G} = NF\,(\eta G N_s)^2 / N_s = \boxed{\langle(\Delta N_s)^2\rangle_\eta\, \eta G^2\, NF}$



Simulation of Preamplified Photodetection of Shot-Noise Limited Signals

- Noise Figure (NF): [PRL 83 (10), pp.1938-1941, Choi, Vasilyev & Kumar]
  - $NF_{tot} = NF_{amp} + (1 - \eta) / (\eta G)$
  - $NF_{PSA} = 1 \rightarrow (NF^{PSA})_{tot} = 1 + (1 - \eta) / (\eta G)$
  - $NF_{PIA} = 2 - 1/G \rightarrow (NF^{PIA})_{tot} = 2 (1 - 1/G) + 1 / (\eta G)$

- Also, the detected signal in each case is different. So, we scale PSA & PIA noise by G^2 in order to fairly compare the photo-current between the three cases.

- Therefore, added noise:
  - No gain $\rightarrow \langle (\Delta N_s)^2 \rangle_\eta$
  - PSA $\rightarrow \eta [1 + (1 - \eta) / (\eta G)] \langle (\Delta N_s)^2 \rangle_\eta$
  - PIA $\rightarrow \eta [2(1 - 1/G) + 1/(\eta G)] \langle (\Delta N_s)^2 \rangle_\eta$

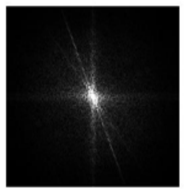
Simulation of Potential Advantage

Although shown here for a spatially broadband case, our goal in the MURI is to do proof-of-principle experiments with raster scanning of the image with use of a fiber-based PSA.

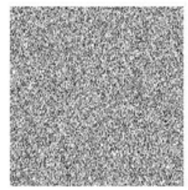
Soft Gaussian Frequency Filter

Start w/ 256 $\times$256 image

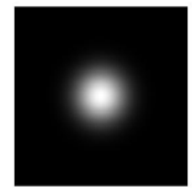
FFT



+



$\times$



Add noise per spatial frequency:

$\langle(\Delta N_s)^2\rangle_\eta \rightarrow$ When G = 1

$\eta\,[1 + (1 - \eta)/(\eta G)]\,\langle(\Delta N_s)^2\rangle_\eta \rightarrow$ For PSA

$\eta\,[\,2(1 - 1/G) + 1/(\eta G)]\,\langle(\Delta N_s)^2\rangle_\eta \rightarrow$ For PIA

IFFT

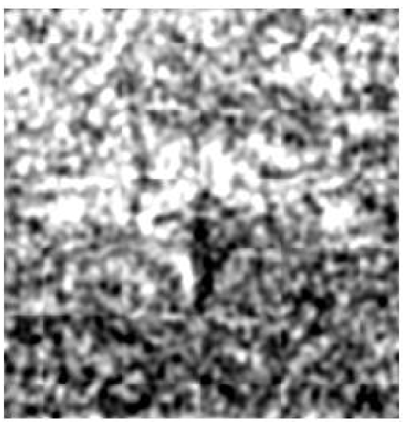
Result

Results: Averaged over 100 Frames
$\eta = 0.8$, G = 10 dB

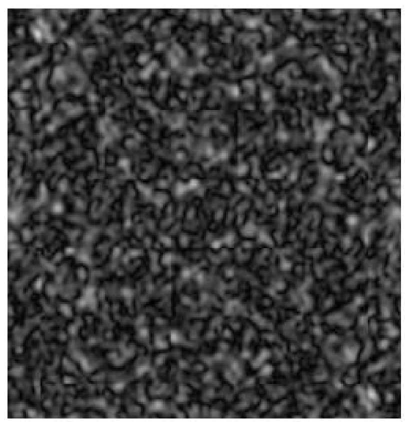
Target (no average)

No gain

PSA gain



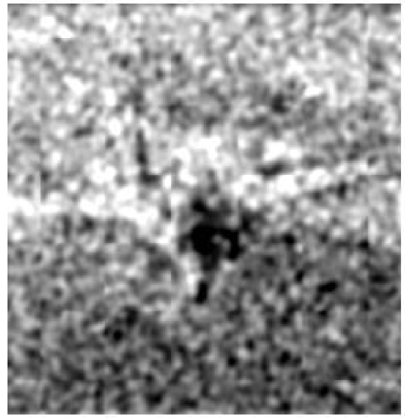
PIA gain



One frame after
IFFT (no average)

Results: Averaged over 100 Frames
η = 0.3, G = 10 dB

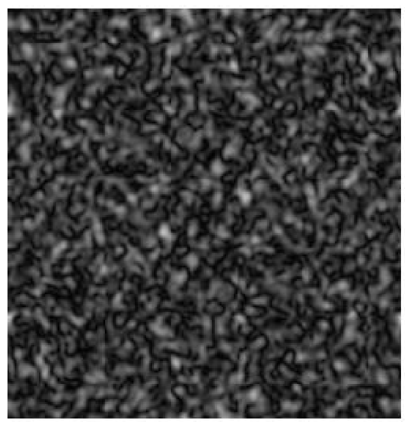
Target (no average)



No gain

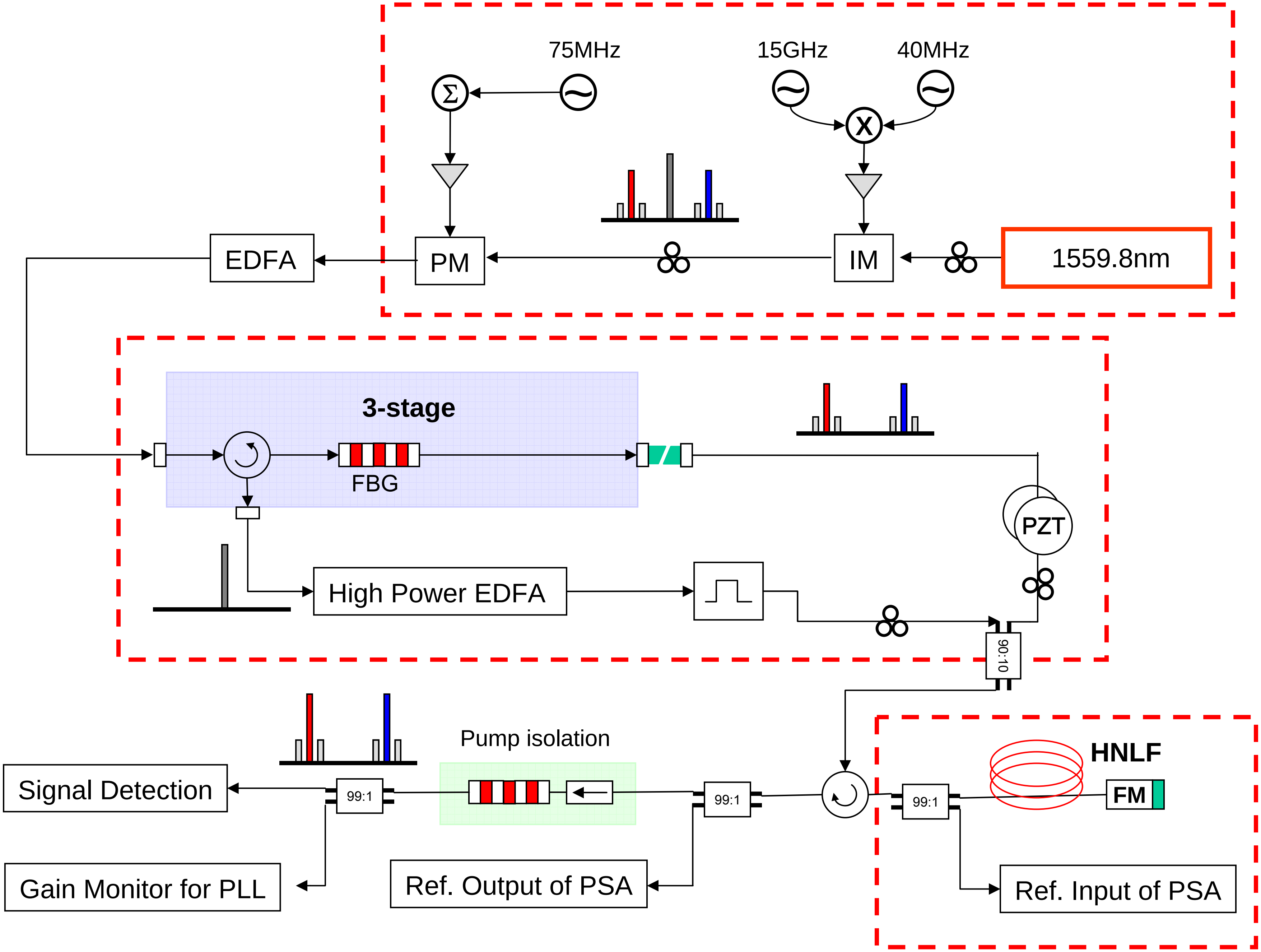
PSA gain

PIA gain

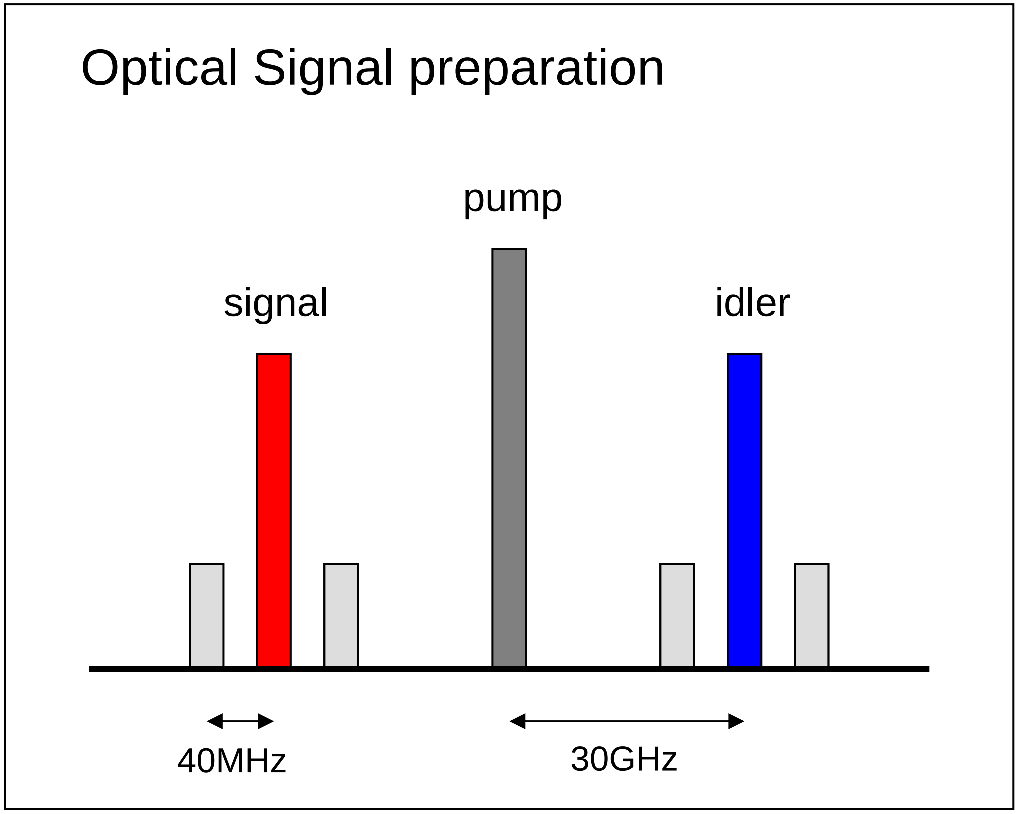


One frame after
IFFT (no average)

Our PSA Experimental Setup

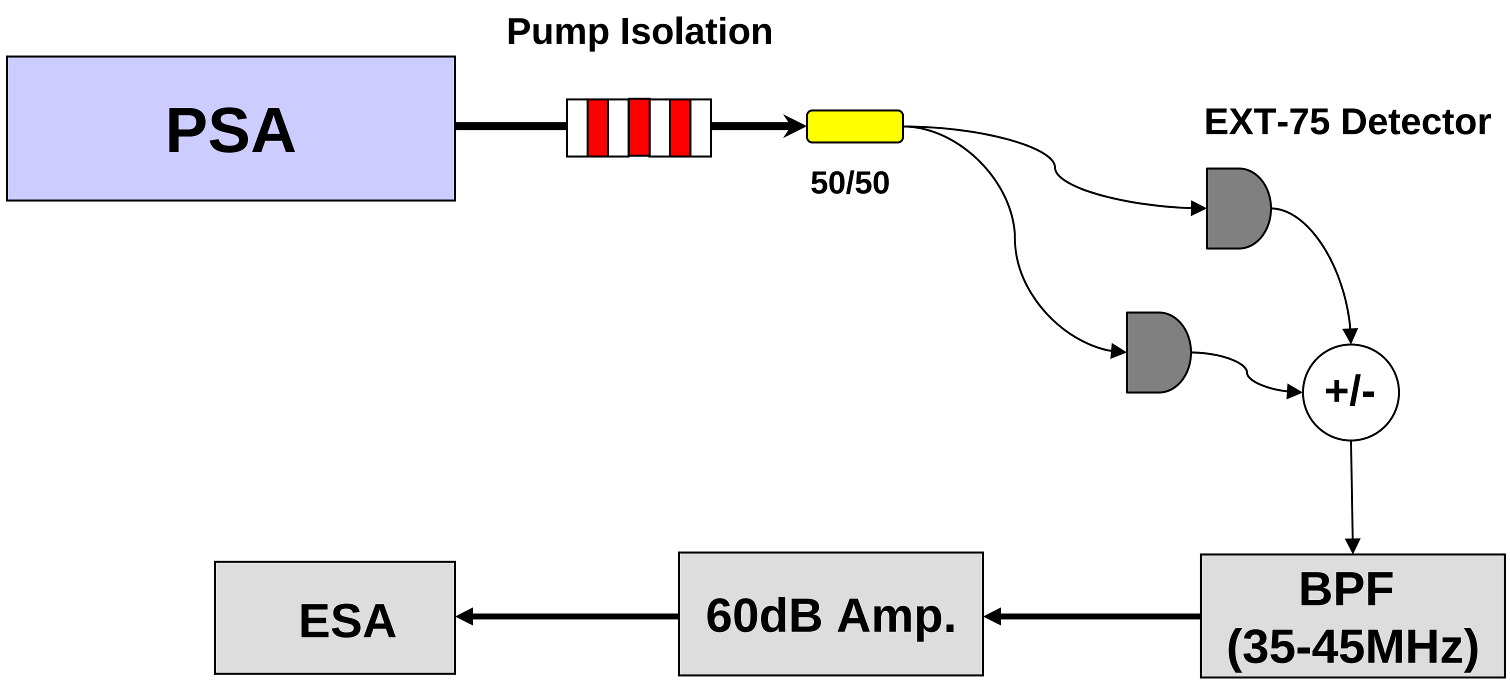


Key Steps in the Measurement Scheme



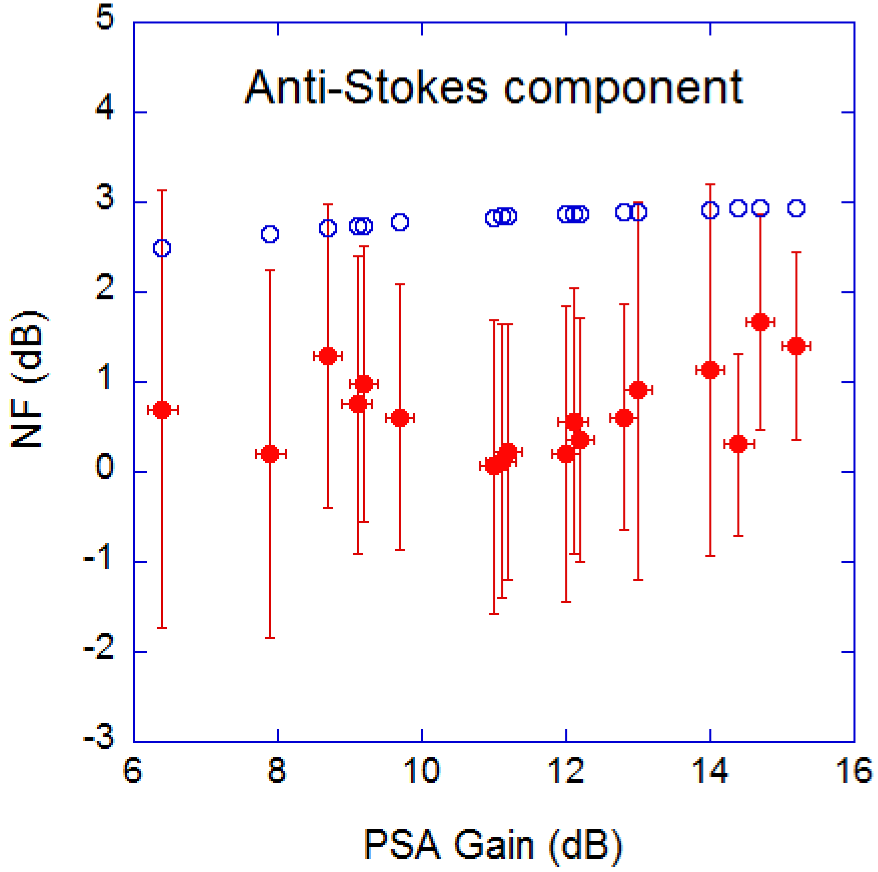
- Employs phase locking loop with piezoelectric transducer for phase-sensitive amplification
- Double pass Highly Nonlinear Fiber
- Noise measurement on the analog signal

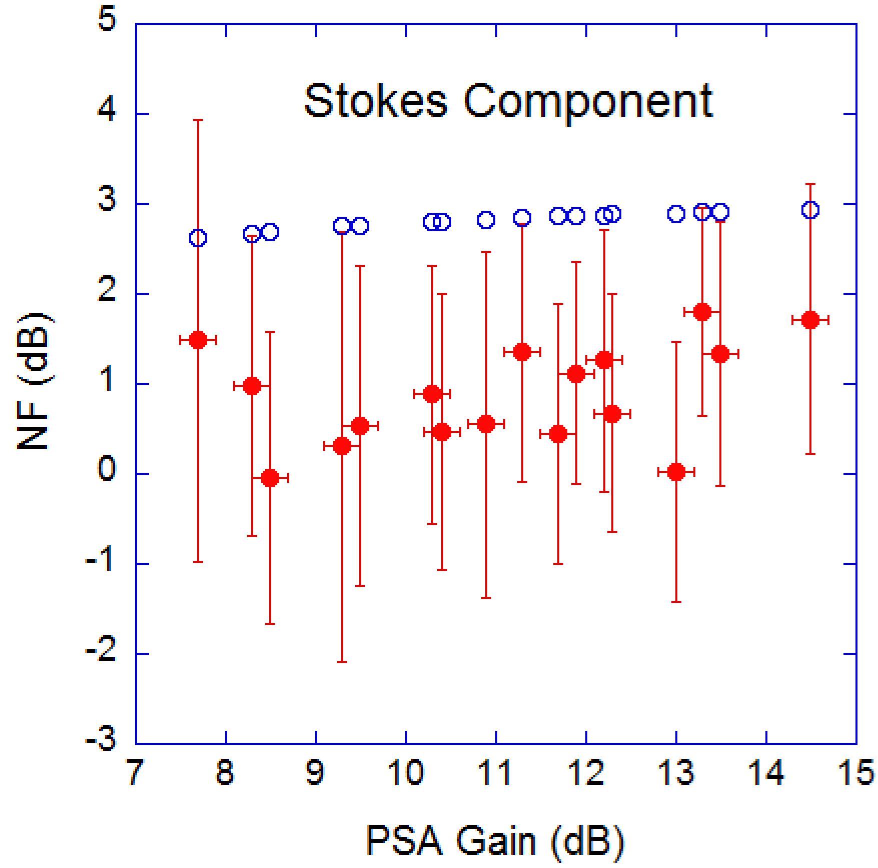
Direct Signal and Noise Measurements



Noise Figure Measurement of the Fiber PSA

Lim, Grigoryan, Shin, & Kumar, OFC'2008





NF_{ave} (Anti-Stokes) = (0.42 ± 0.53) dB

NF_{ave} (Stokes) = (0.68 ± 0.59) dB

Proposed Proof-of-Principle Experiment

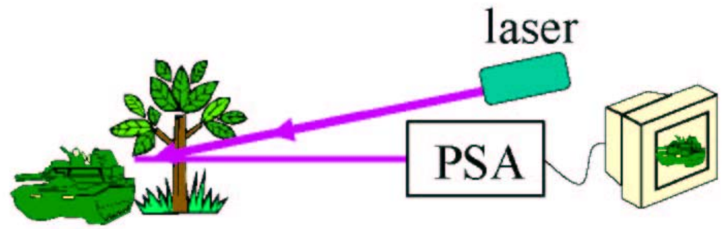
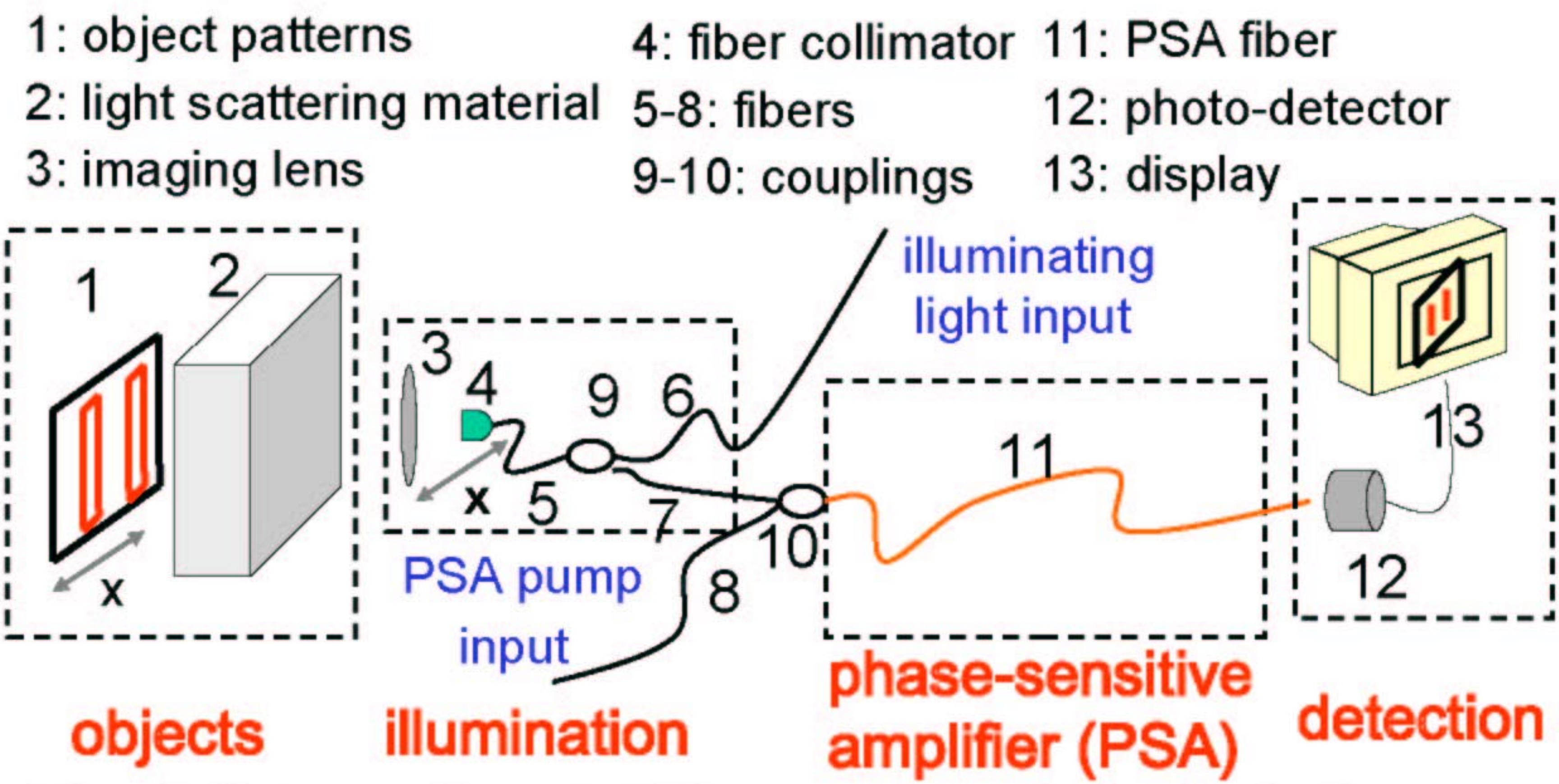


Fig. 1 Cartoon illustrating the real situations where PSA finds useful applications.



Experiment in Progress