

Quantum Imaging and Slow and Fast light

Robert W. Boyd

Institute of Optics and
Department of Physics and Astronomy
University of Rochester

www.optics.rochester.edu/~boyd

Presented at the University of Erlangen-Nürnberg, February 26, 2007.

Interest in Slow Light

Intrigue: Can (group) refractive index really be 10^6 ?

Fundamentals of optical physics

Optical delay lines, optical storage, optical memories

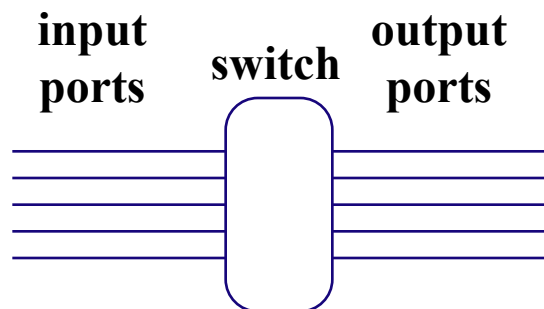
Implications for quantum information

What about fast light ($v > c$) and backwards light (v negative)?

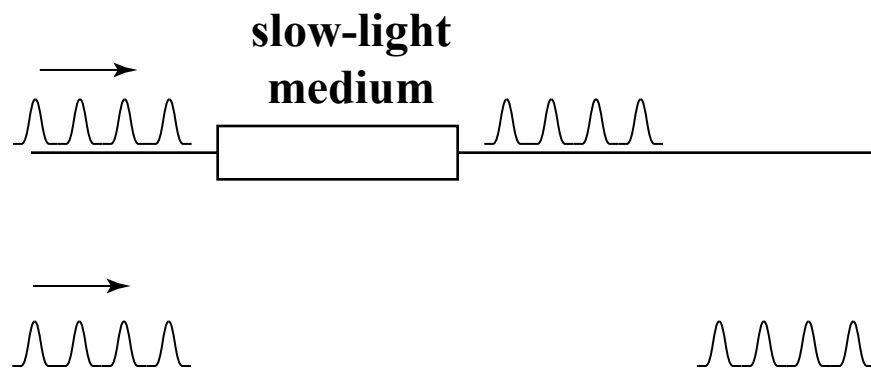
Boyd and Gauthier, "Slow and Fast Light," in Progress in Optics, 43, 2002.



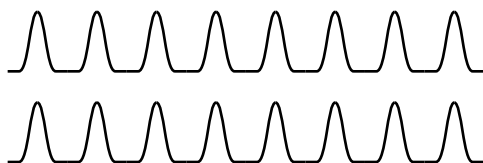
All-Optical Switch



Use Optical Buffering to Resolve Data-Packet Contention



But what happens if two data packets arrive simultaneously?



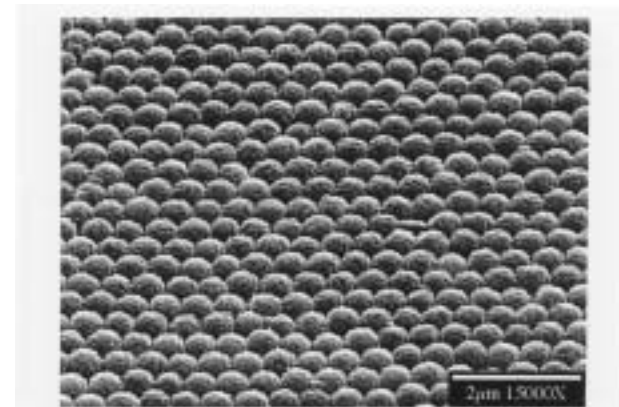
Controllable slow light can dramatically increase system performance.

Key figure of merit: number of pulse widths of delay.

Some Approaches to Slow Light Propagation

- Use the linear response of atomic systems
or (better)
use quantum coherence (e.g., electromagnetically induced transparency) to modify and control this response
- Use of artificial materials (to modify the optical properties at the macroscopic level)

E.g., photonic crystals where strong spectral variation of the refractive index occurs near the edge of the photonic bandgap



polystyrene photonic crystal

Slow and Fast Light and Optical Resonances

Pulses propagate at the group velocity given by

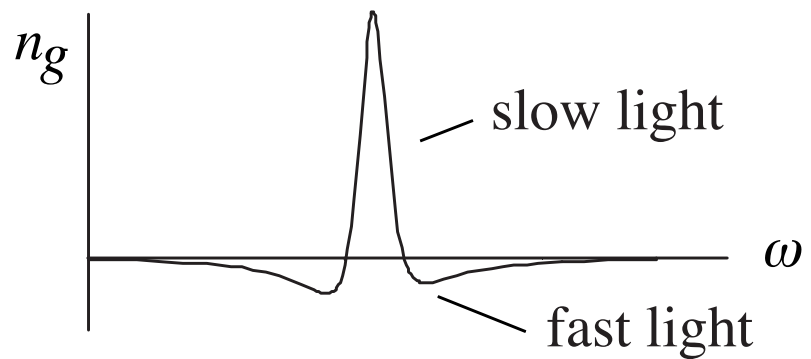
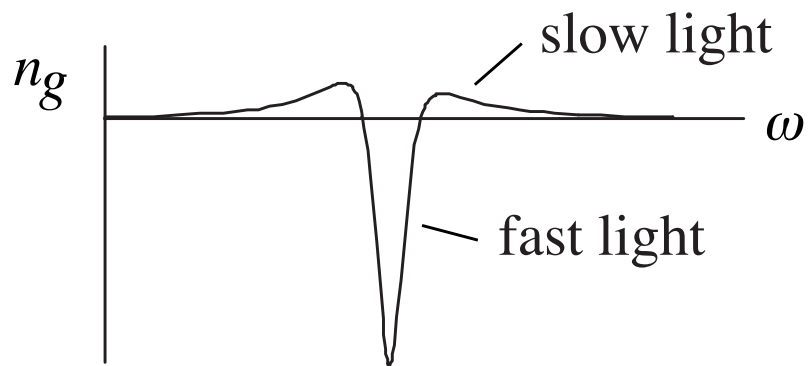
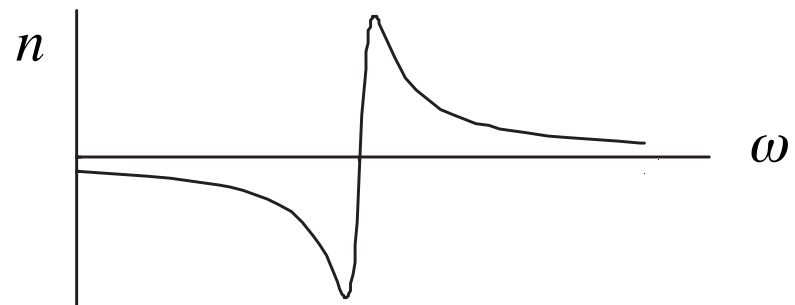
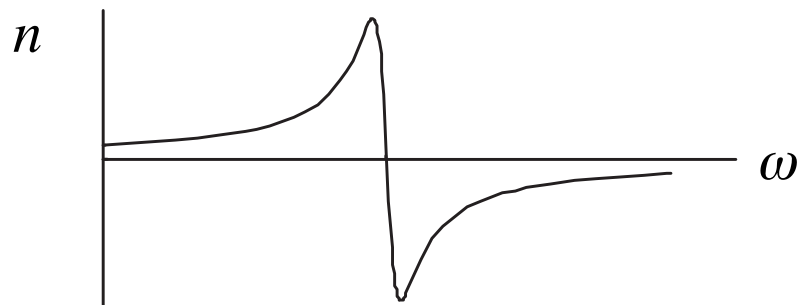
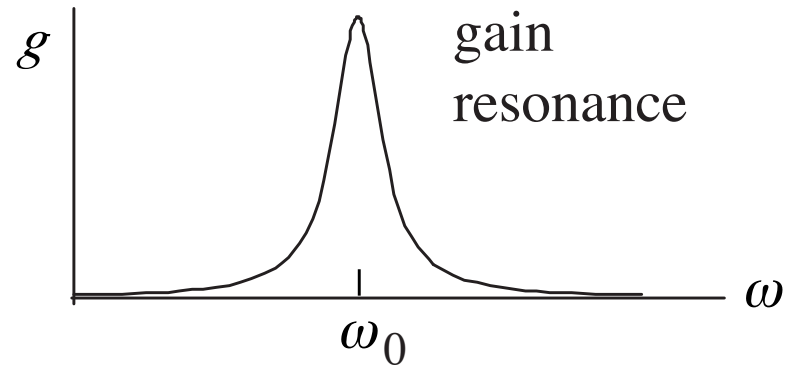
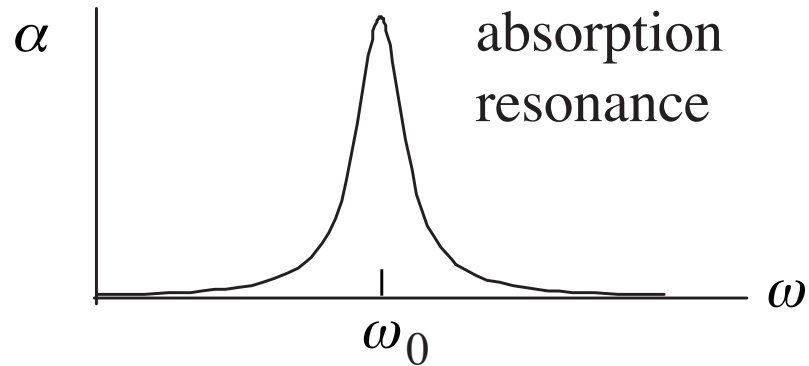
$$v_g = \frac{c}{n_g} \quad n_g = n + \omega \frac{dn}{d\omega}$$

Want large dispersion to obtain extreme group velocities

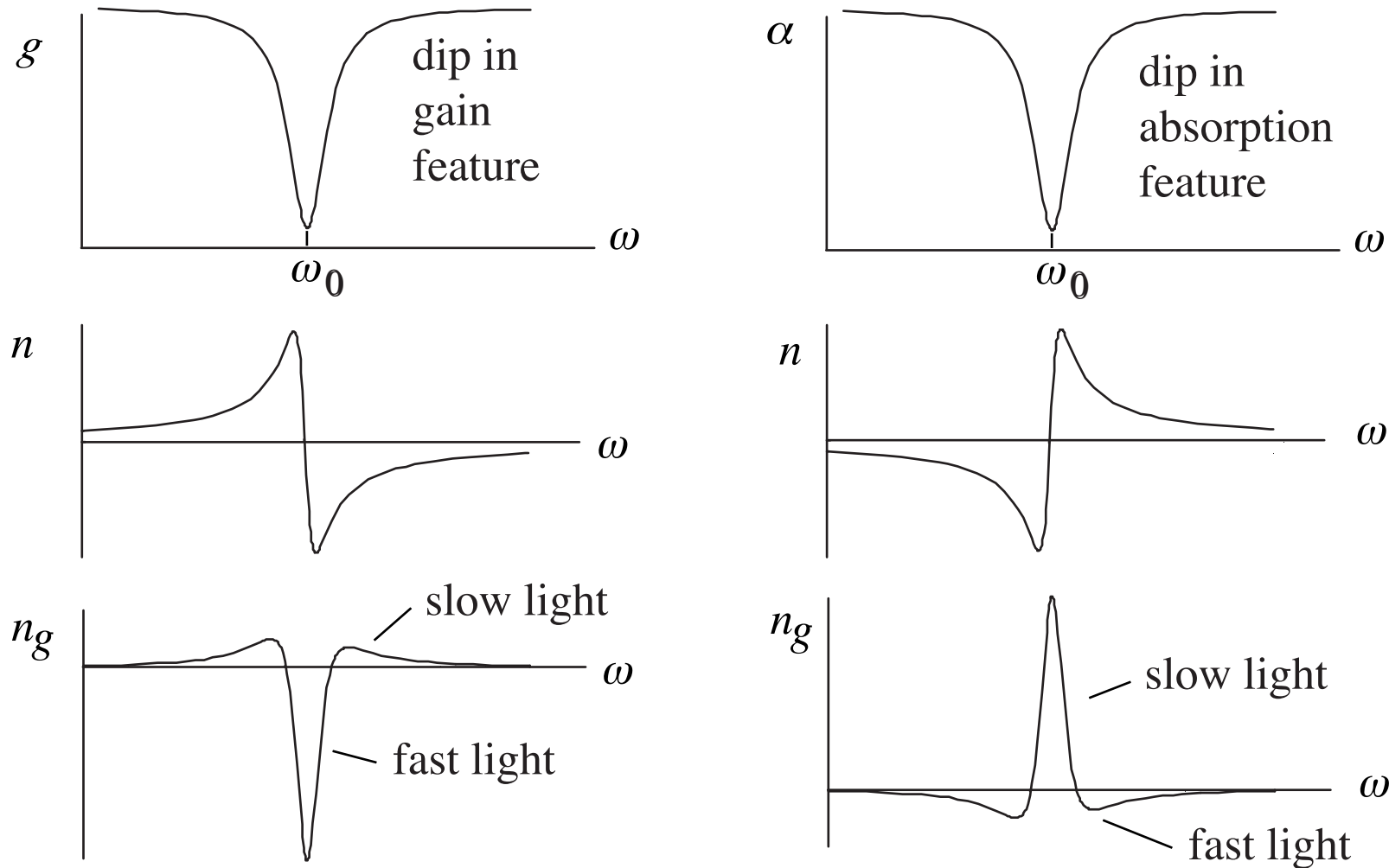
Sharp spectral features produce large dispersion.

The group index can be large and positive (slow light), positive and much less than unity (fast light) or negative (backwards light).

How to Create Slow and Fast Light I – Use Isolated Gain or Absorption Resonance

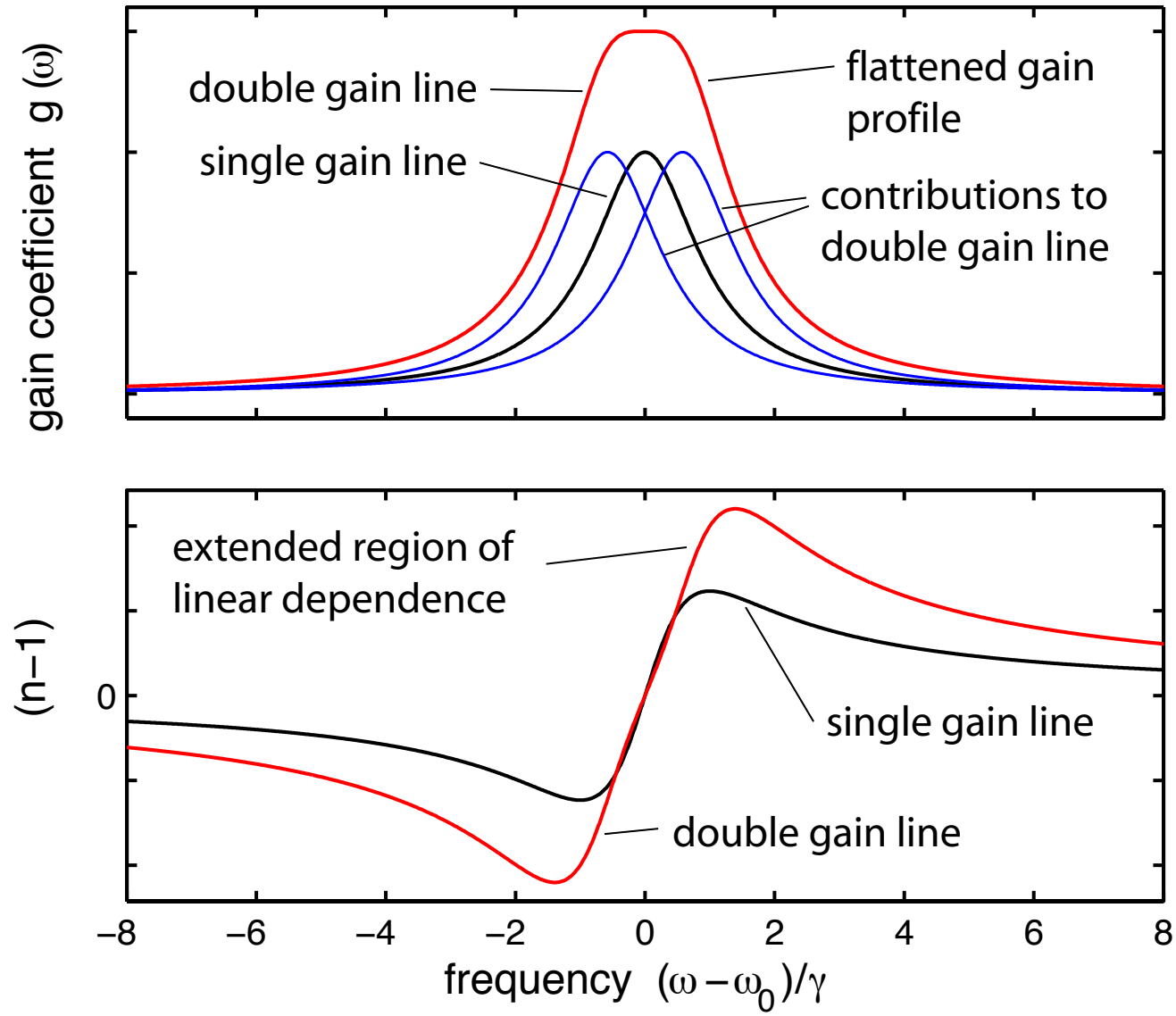


How to Create Slow and Fast Light II – Use Dip in Gain or Absorption Feature



Narrow dips in gain and absorption lines can be created by various nonlinear optical effects, such as electromagnetically induced transparency (EIT), coherent population oscillations (CPO), and conventional saturation.

How to Create Slow and Fast Light III – Dispersion Management



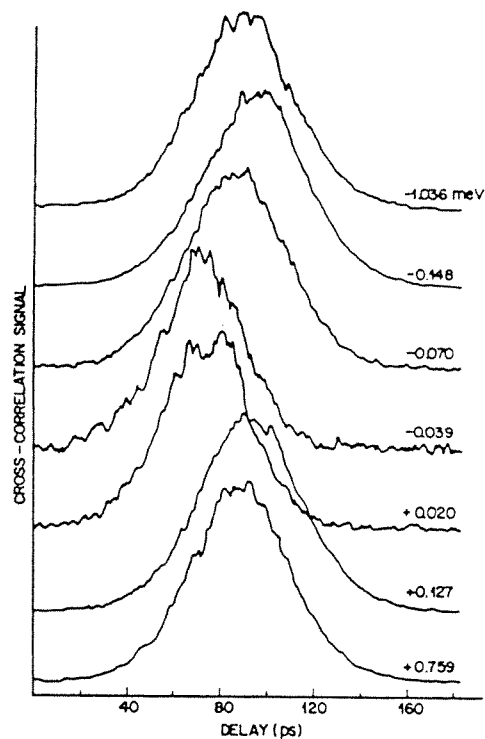
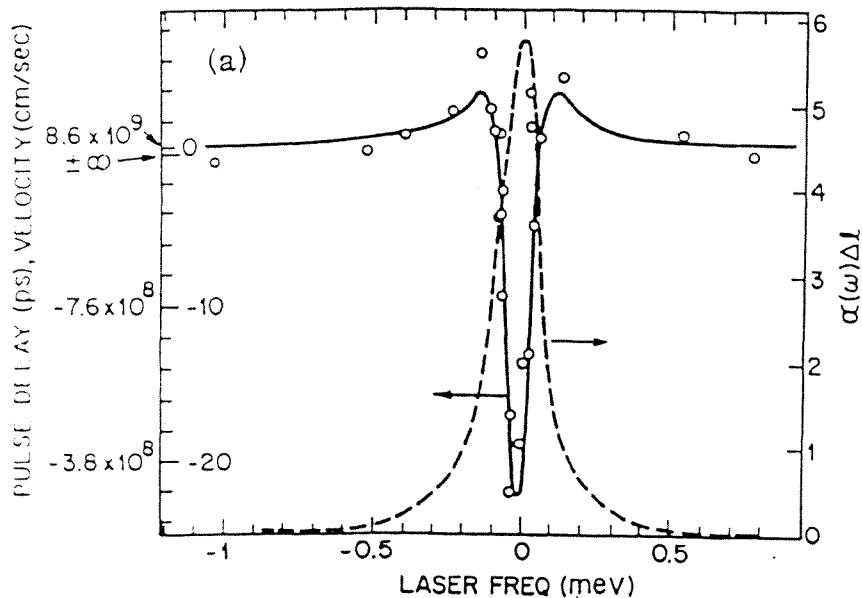
Linear Pulse Propagation in an Absorbing Medium

S. Chu and S. Wong

Bell Laboratories, Murray Hill, New Jersey 07974

(Received 30 November 1981)

The pulse velocity in the linear regime in samples of GaP:N with a laser tuned to the bound A-exciton line is measured with use of a picosecond time-of-flight technique. The pulse is seen to propagate through the material with little pulse-shape distortion, and with an envelope velocity given by the group velocity even when the group velocity exceeds 3×10^{10} cm/sec, equals $\pm \infty$, or becomes negative. The results verify the predictions of Garrett and McCumber.



Light speed reduction to 17 metres per second in an ultracold atomic gas

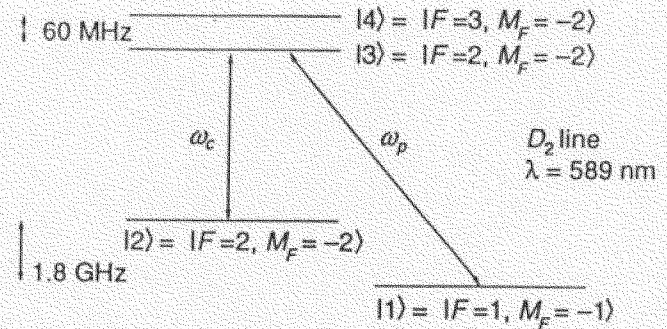
Lene Vestergaard Hau^{*†}, S. E. Harris[‡], Zachary Dutton^{*†}
& Cyrus H. Behroozi^{*§}

^{*} Rowland Institute for Science, 100 Edwin H. Land Boulevard, Cambridge,
Massachusetts 02142, USA

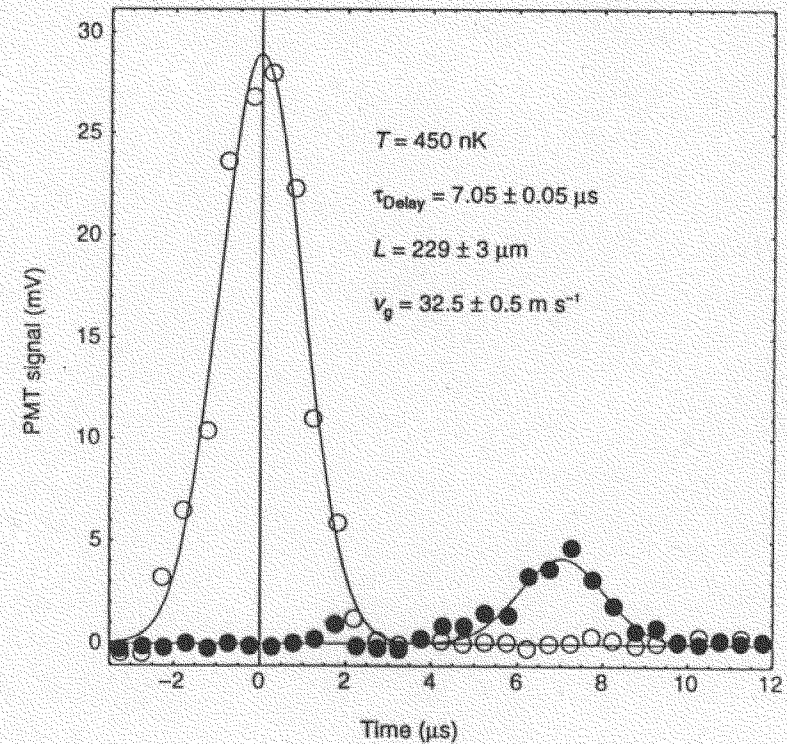
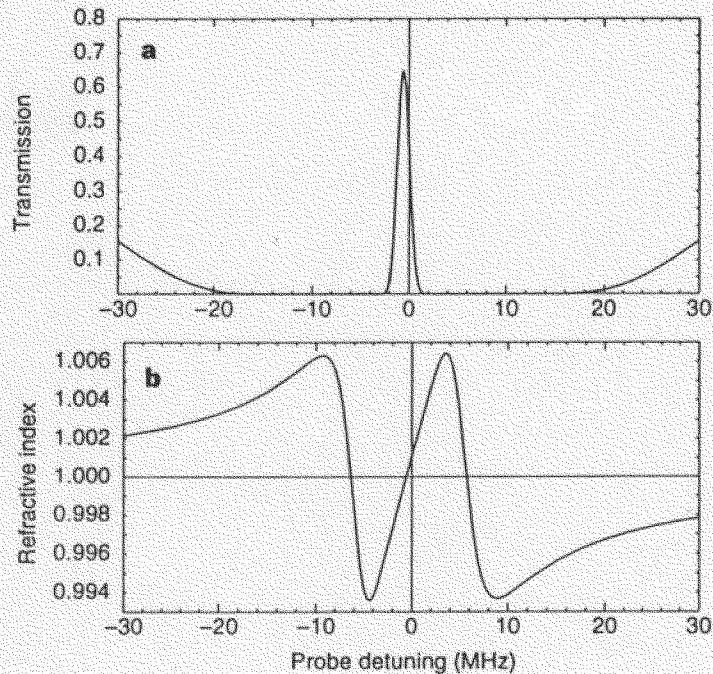
[†] Department of Physics, [§] Division of Engineering and Applied Sciences,
Harvard University, Cambridge, Massachusetts 02138, USA

[‡] Edward L. Ginzton Laboratory, Stanford University, Stanford, California 94305,
USA

Nature, 397, 594, (1999).



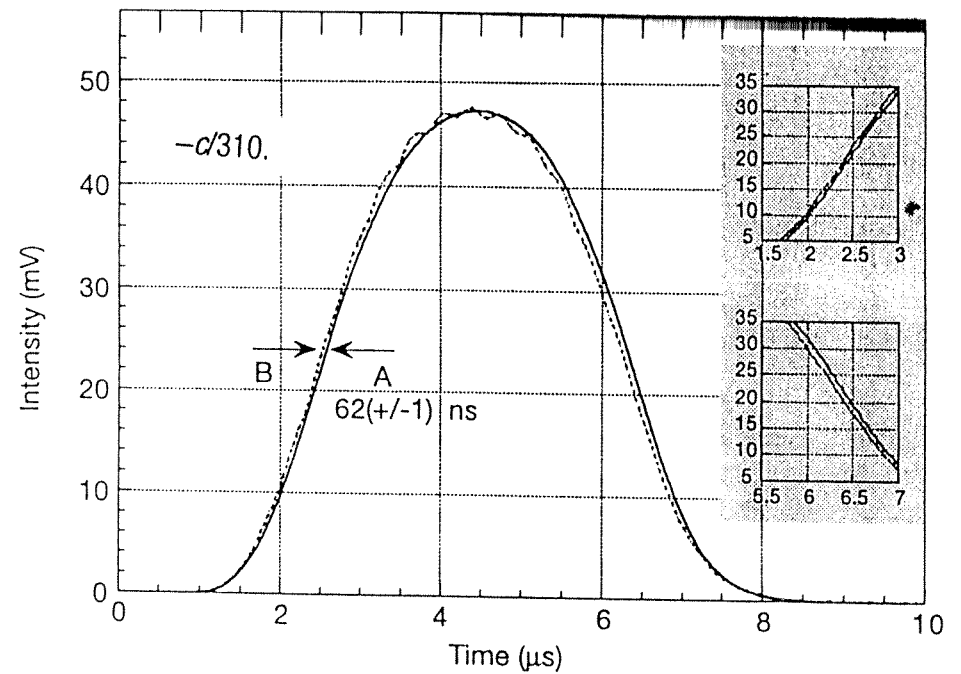
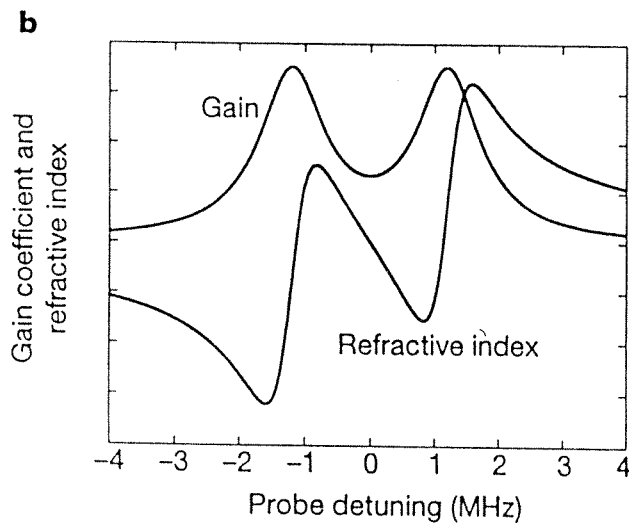
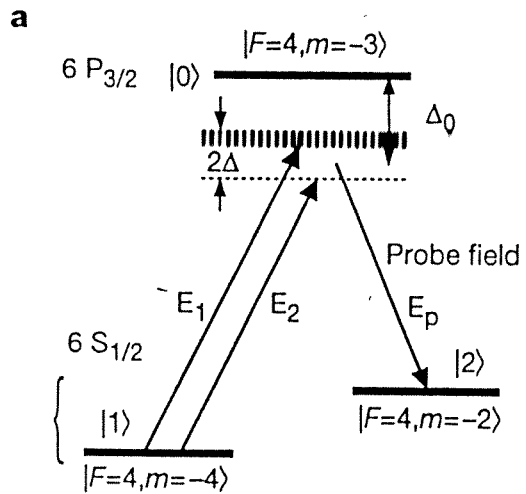
$$v_g = \frac{c}{n(\omega_p) + \omega_p \frac{dn}{d\omega_p}} \approx \frac{\hbar c \epsilon_0 |\Omega_c|^2}{2\omega_p |\mu_{13}|^2 N}$$



Gain-assisted superluminal light propagation

L. J. Wang, A. Kuzmich & A. Dogariu

NEC Research Institute, 4 Independence Way, Princeton, New Jersey 08540, USA



Challenge / Goal (2003)

Slow light is a room-temperature, solid-state material.

Our solution:

Slow light *via* coherent population oscillations (CPO), a quantum coherence effect related to EIT but which is less sensitive to dephasing processes.

Slow Light in Ruby

Recall that $n_g = n + \omega(dn/d\omega)$. Need a large $dn/d\omega$. (How?)

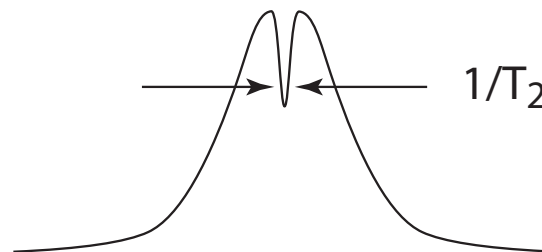
Kramers-Kronig relations:

Want a very narrow feature in absorption line.

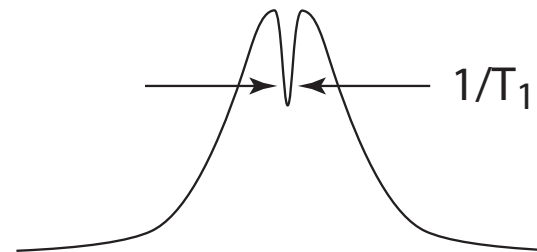
Well-known “trick” for doing so:

Make use of spectral holes due to population oscillations.

Hole-burning in a homogeneously broadened line; requires $T_2 \ll T_1$.

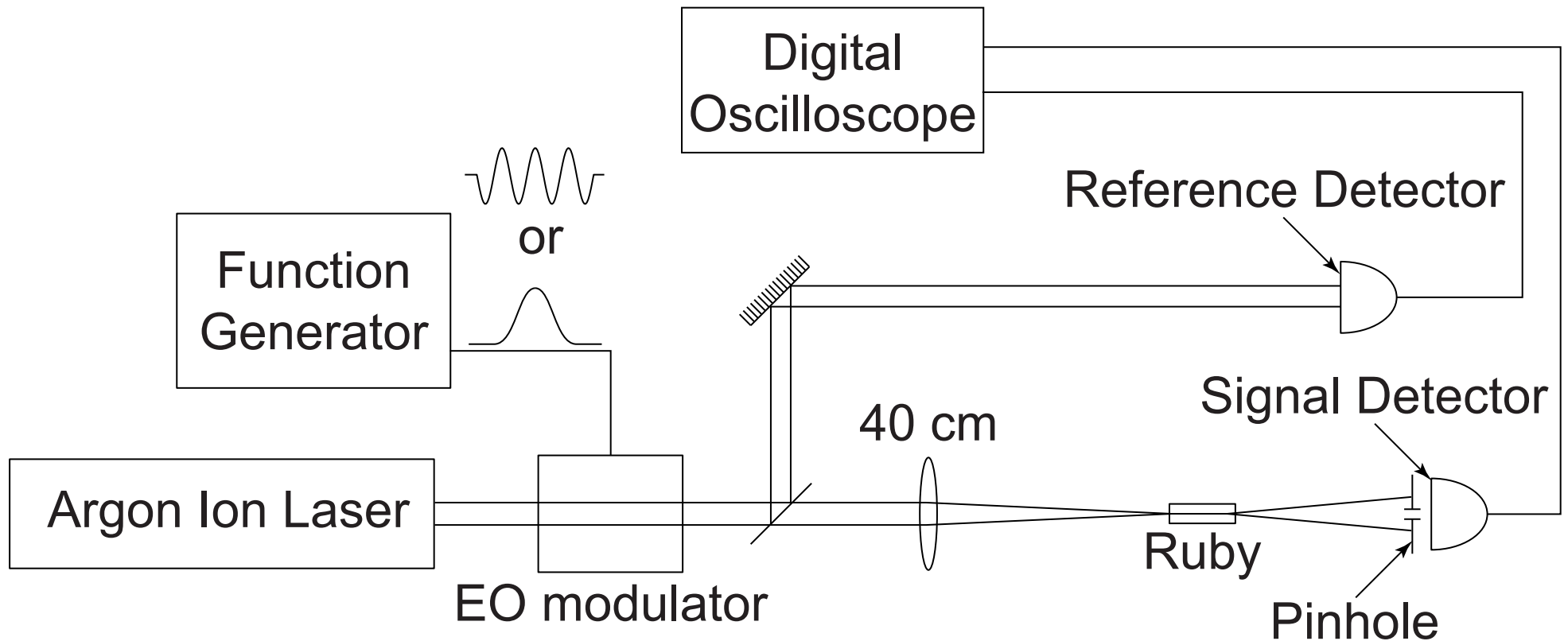


inhomogeneously
broadened medium



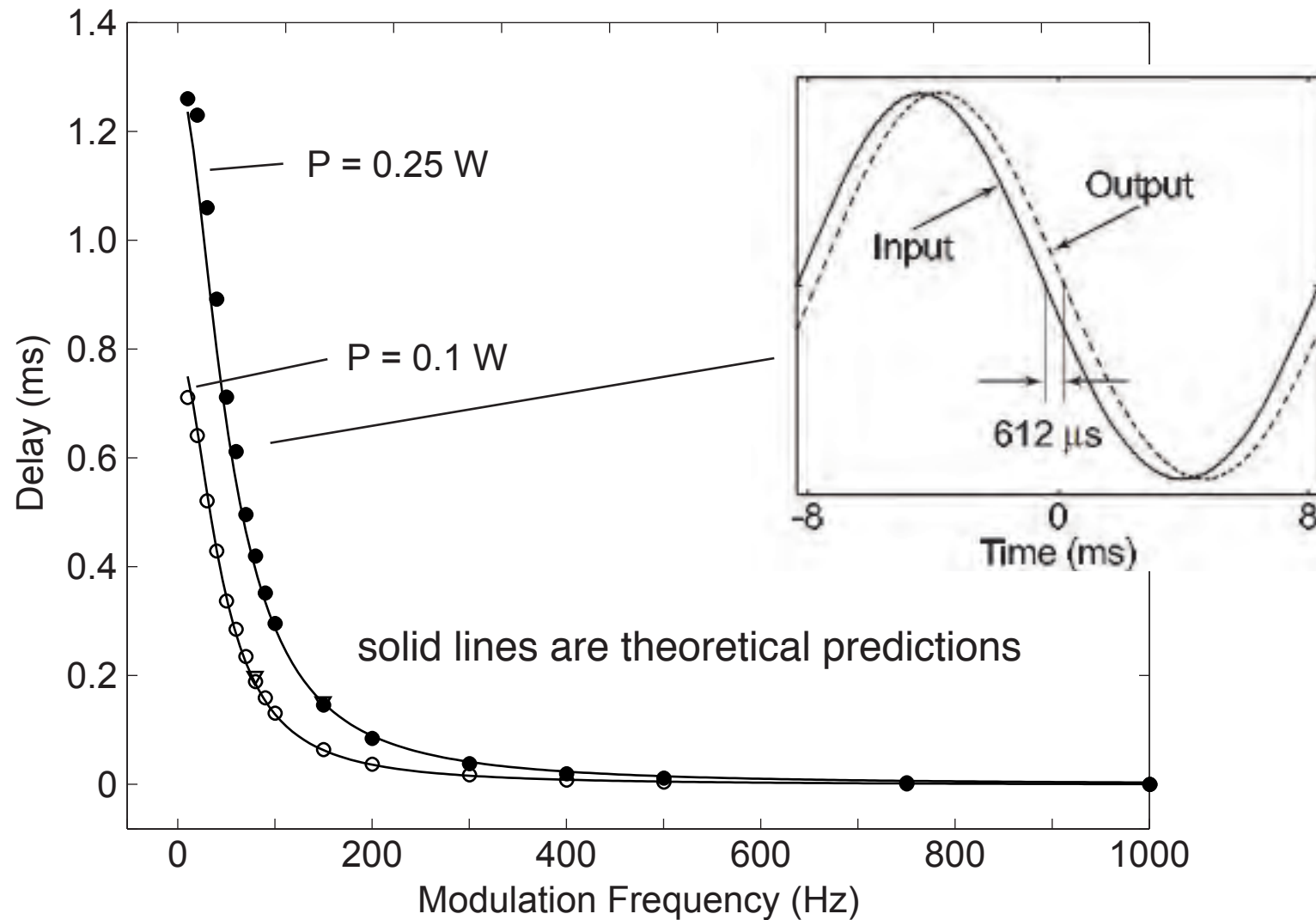
homogeneously
broadened medium
(or inhomogeneously
broadened)

Slow Light Experimental Setup



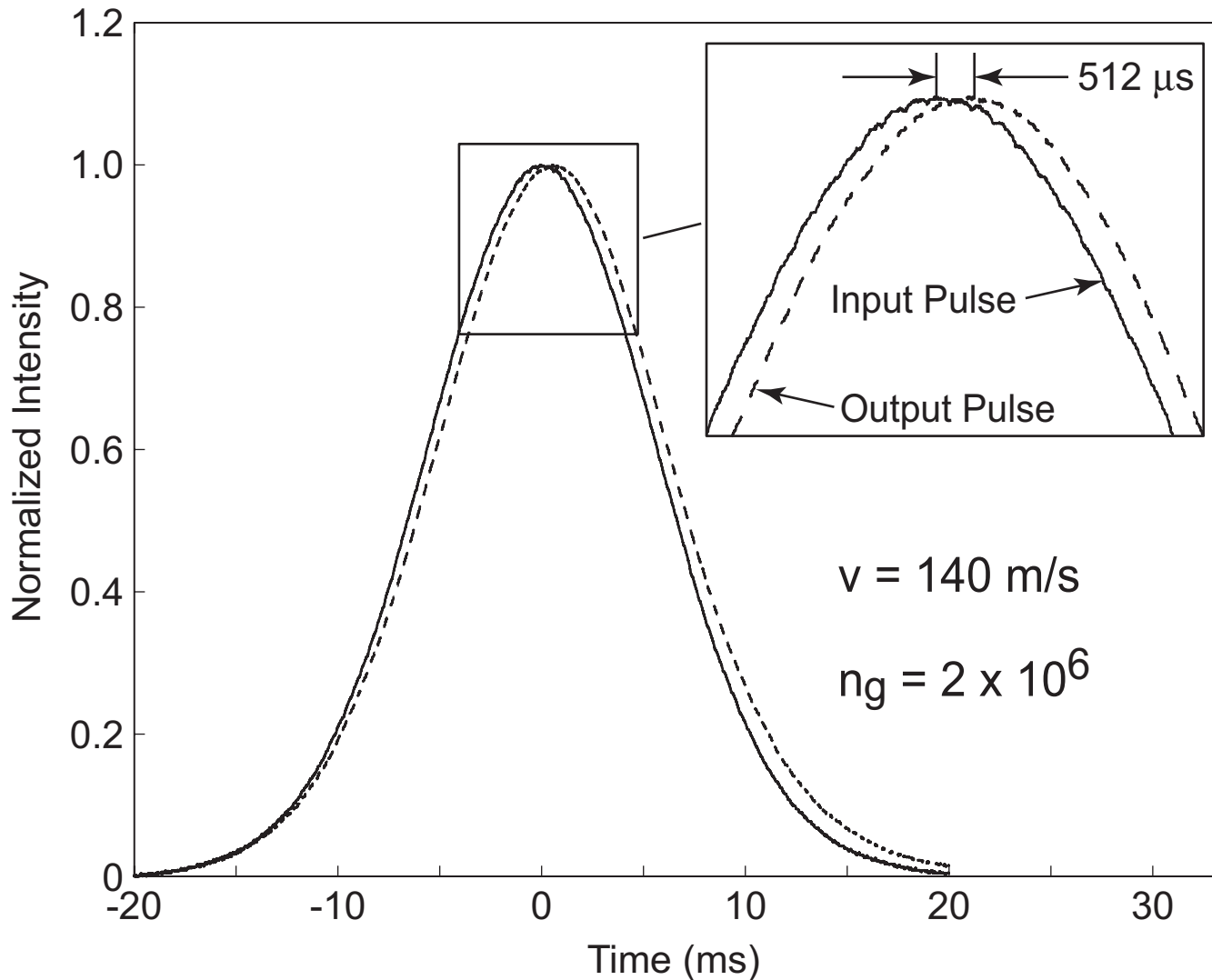
7.25-cm-long ruby laser rod (pink ruby)

Measurement of Delay Time for Harmonic Modulation



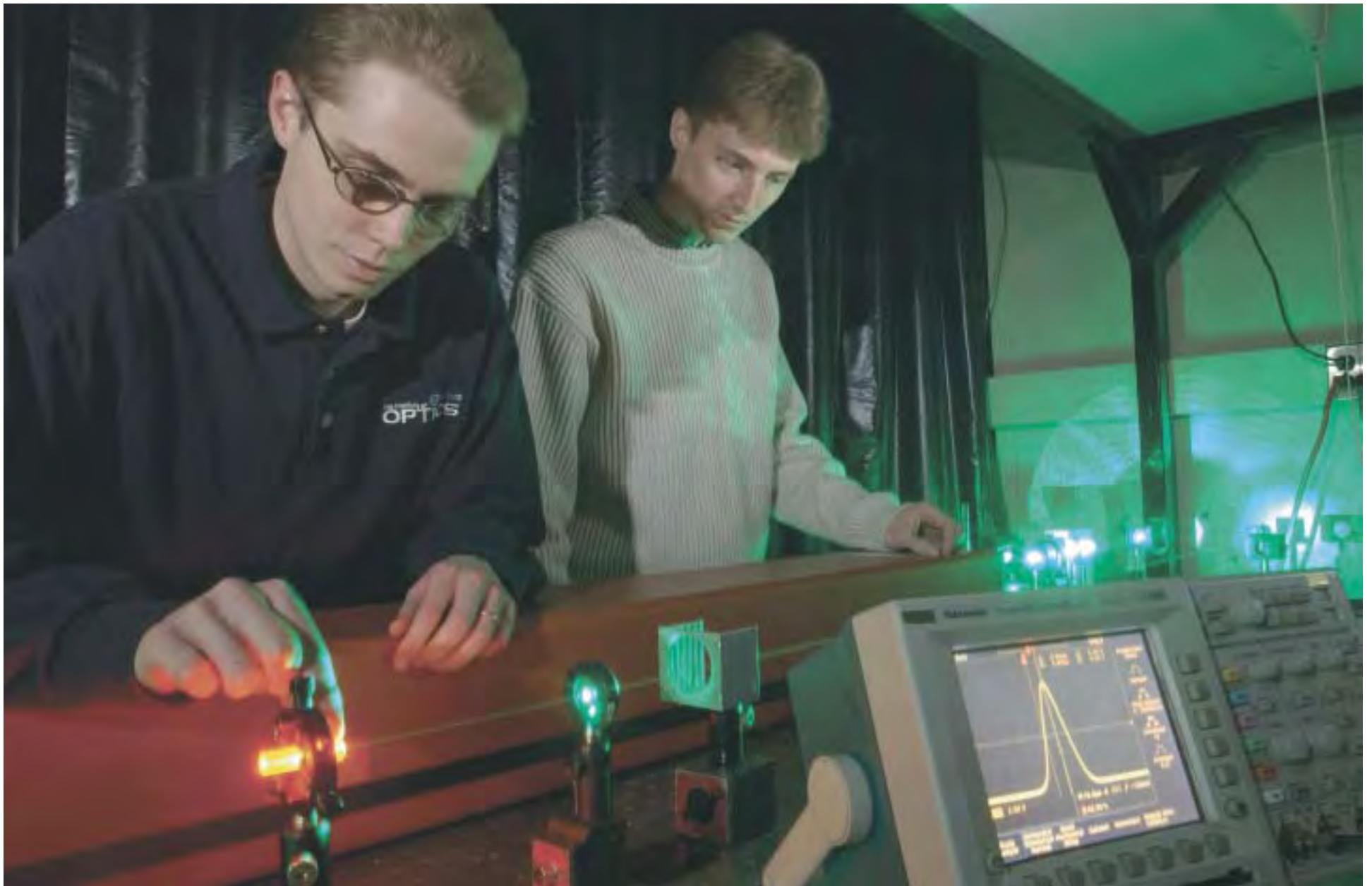
For 1.2 ms delay, $v = 60$ m/s and $n_g = 5 \times 10^6$

Gaussian Pulse Propagation Through Ruby



No pulse distortion!

Matt Bigelow and Nick Lepeshkin in the Lab



Advantages of Coherent Population Oscillations for Slow Light

Works in solids

Works at room temperature

Insensitive of dephasing processes

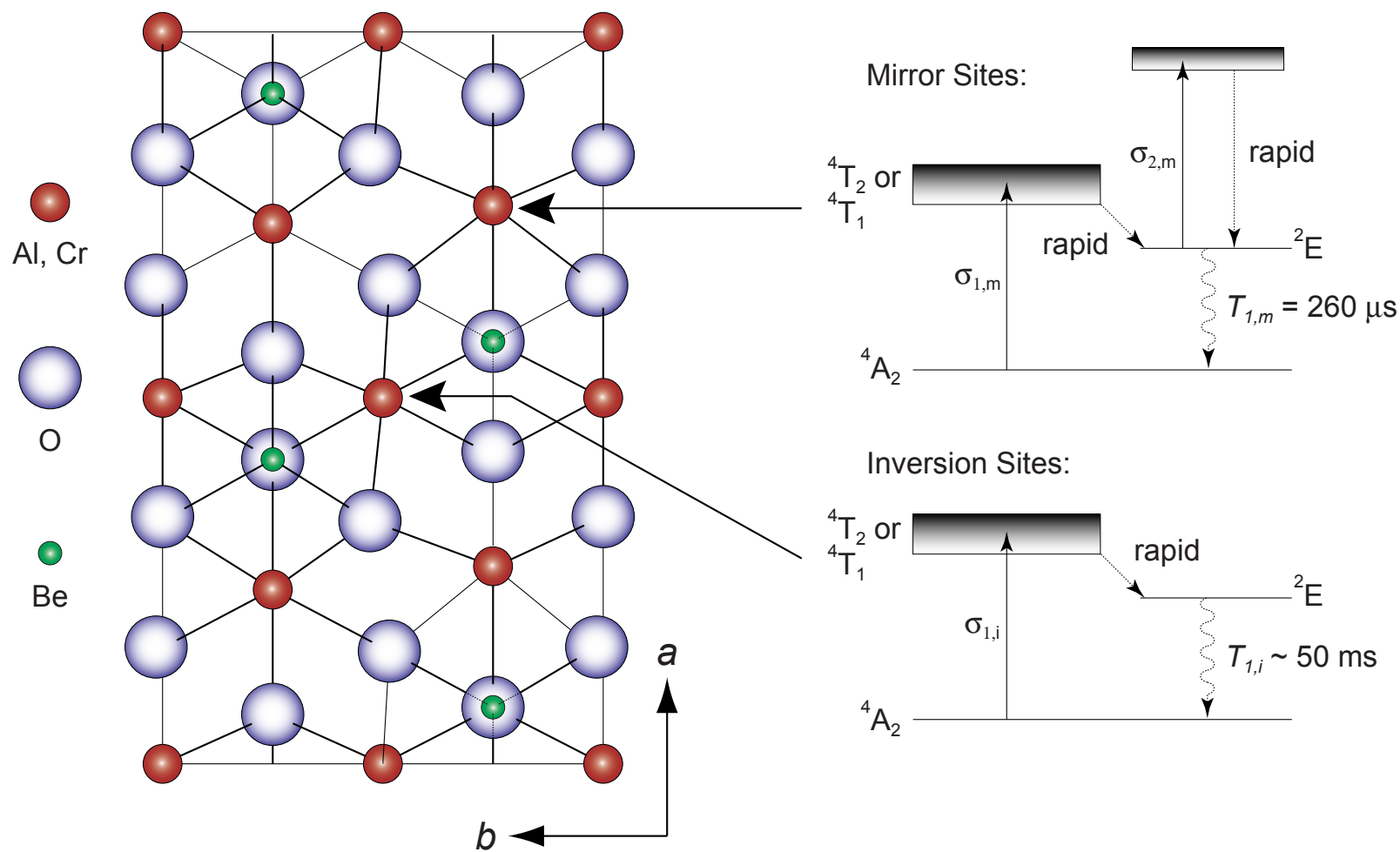
Laser need not be frequency stabilized

Works with single beam (self-delayed)

Delay can be controlled through input intensity

Alexandrite Displays both Saturable and Reverse-Saturable Absorption

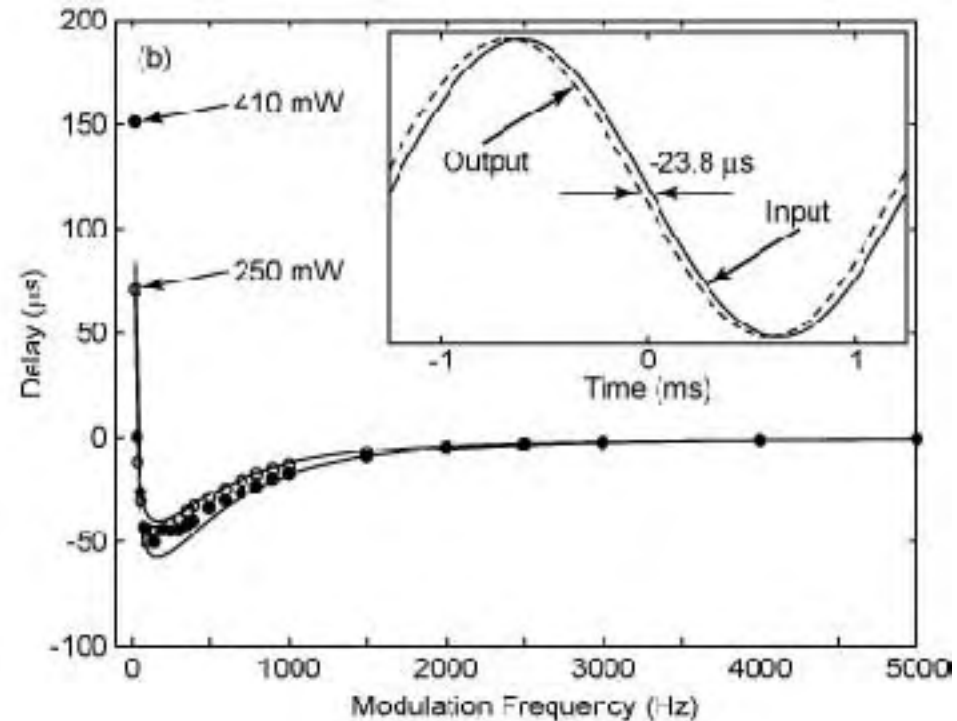
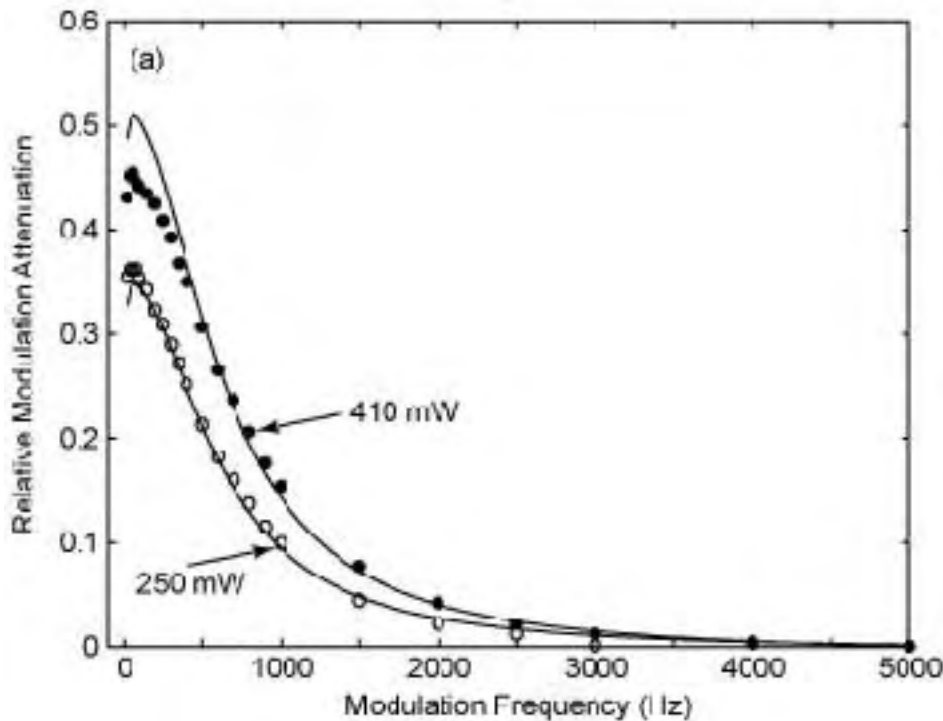
- Both slow and fast propagation observed in alexandrite



Inverse-Saturable Absorption Produces Superluminal Propagation in Alexandrite

At 476 nm, alexandrite is an inverse saturable absorber

Negative time delay of 50 μs corresponds to a velocity of -800 m/s



M. Bigelow, N. Lepeshkin, and RWB, Science, 2003

Numerical Modeling of Pulse Propagation through Slow and Fast-Light Media

Numerically integrate the reduced wave equation

$$\frac{\partial A}{\partial z} - \frac{1}{v_g} \frac{\partial A}{\partial t} = 0$$

and plot $A(z,t)$ versus distance z .

Assume an input pulse with a Gaussian temporal profile.

Study three cases:

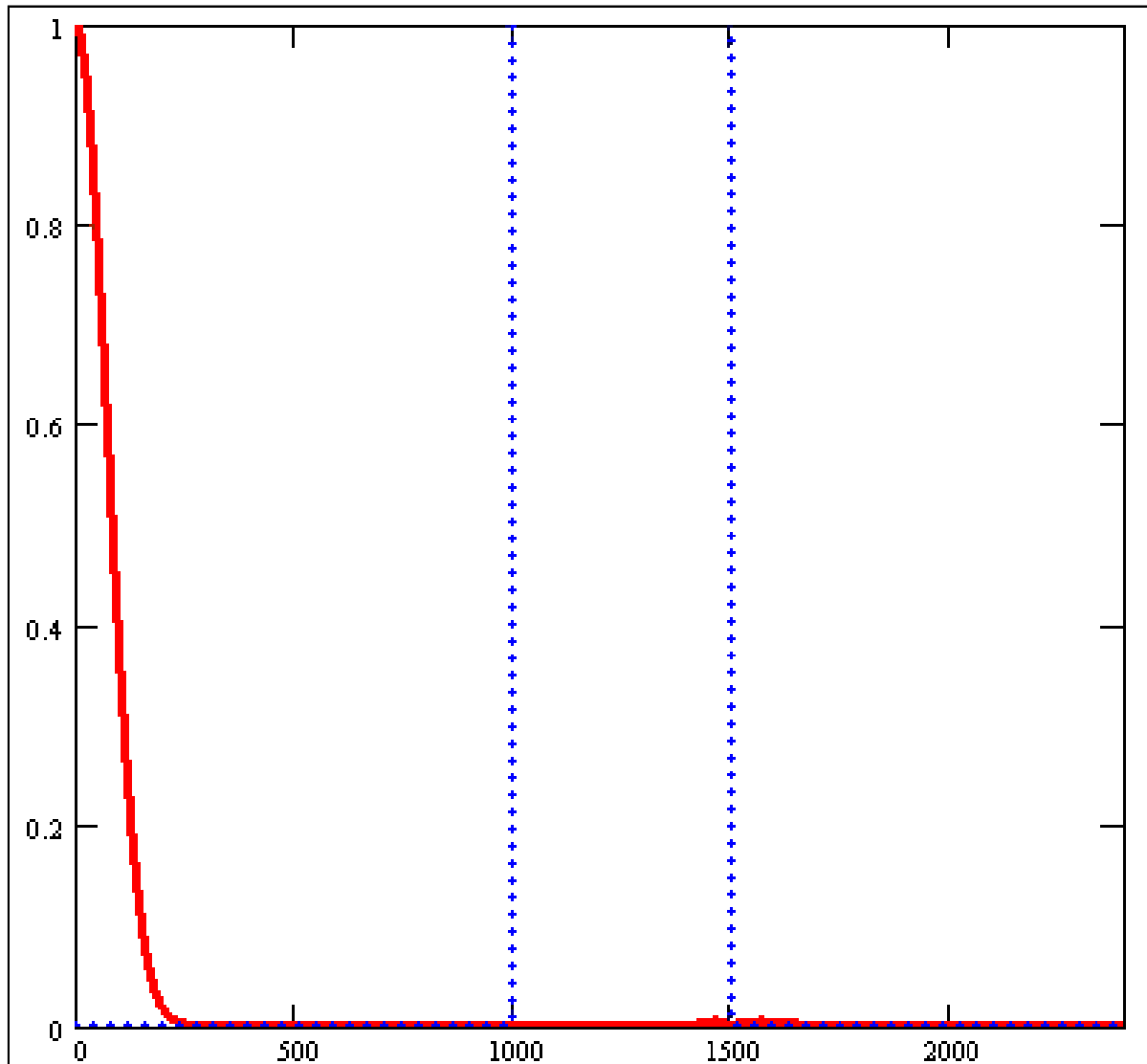
Slow light $v_g = 0.5 c$

Fast light $v_g = 5 c$ and $v_g = -2 c$

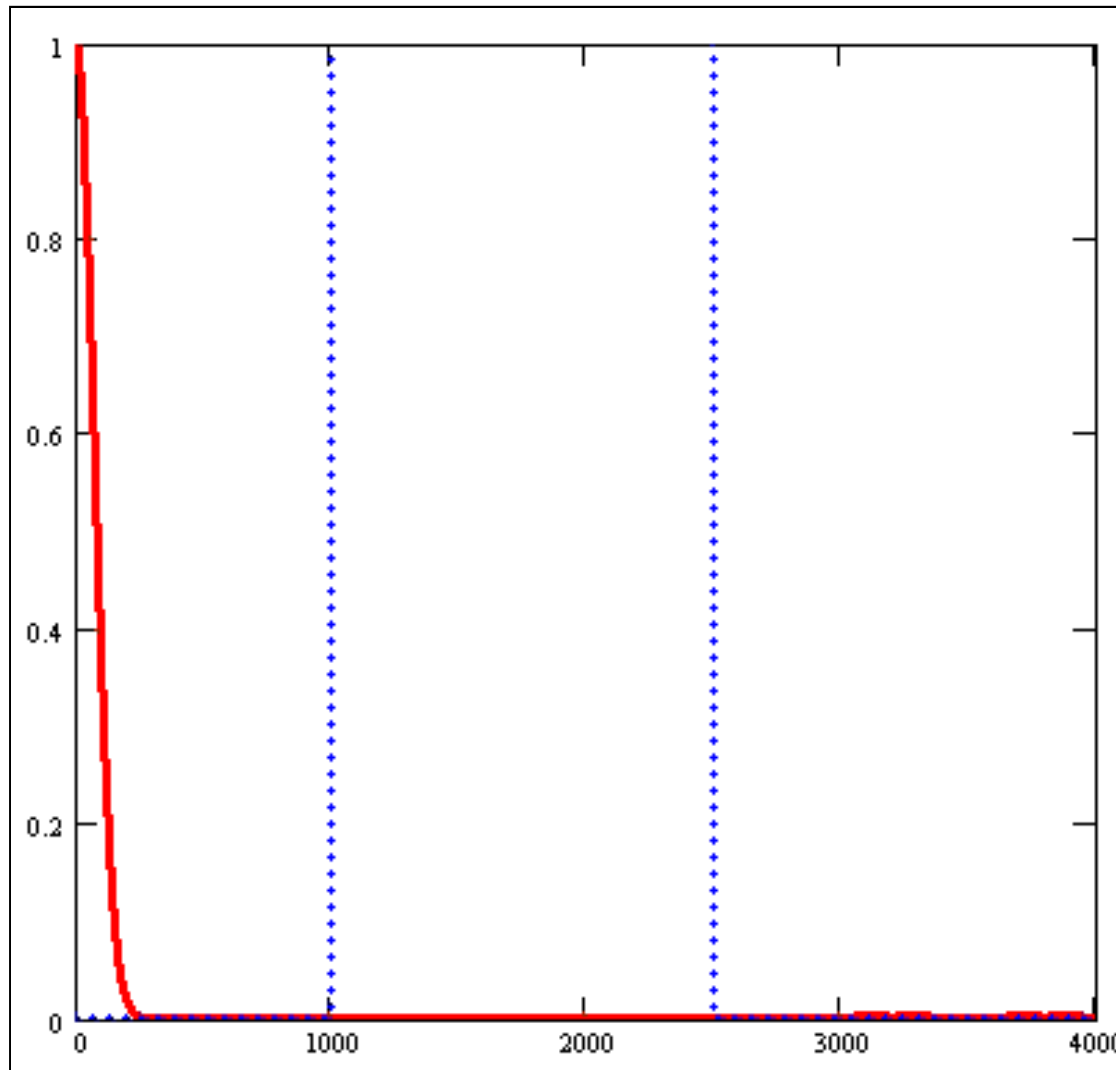
CAUTION: This is a very simplistic model. It ignores GVD and spectral reshaping.

See also Dogariu et al. Opt. Express 8, 344 (2001) and Milonni (2005).

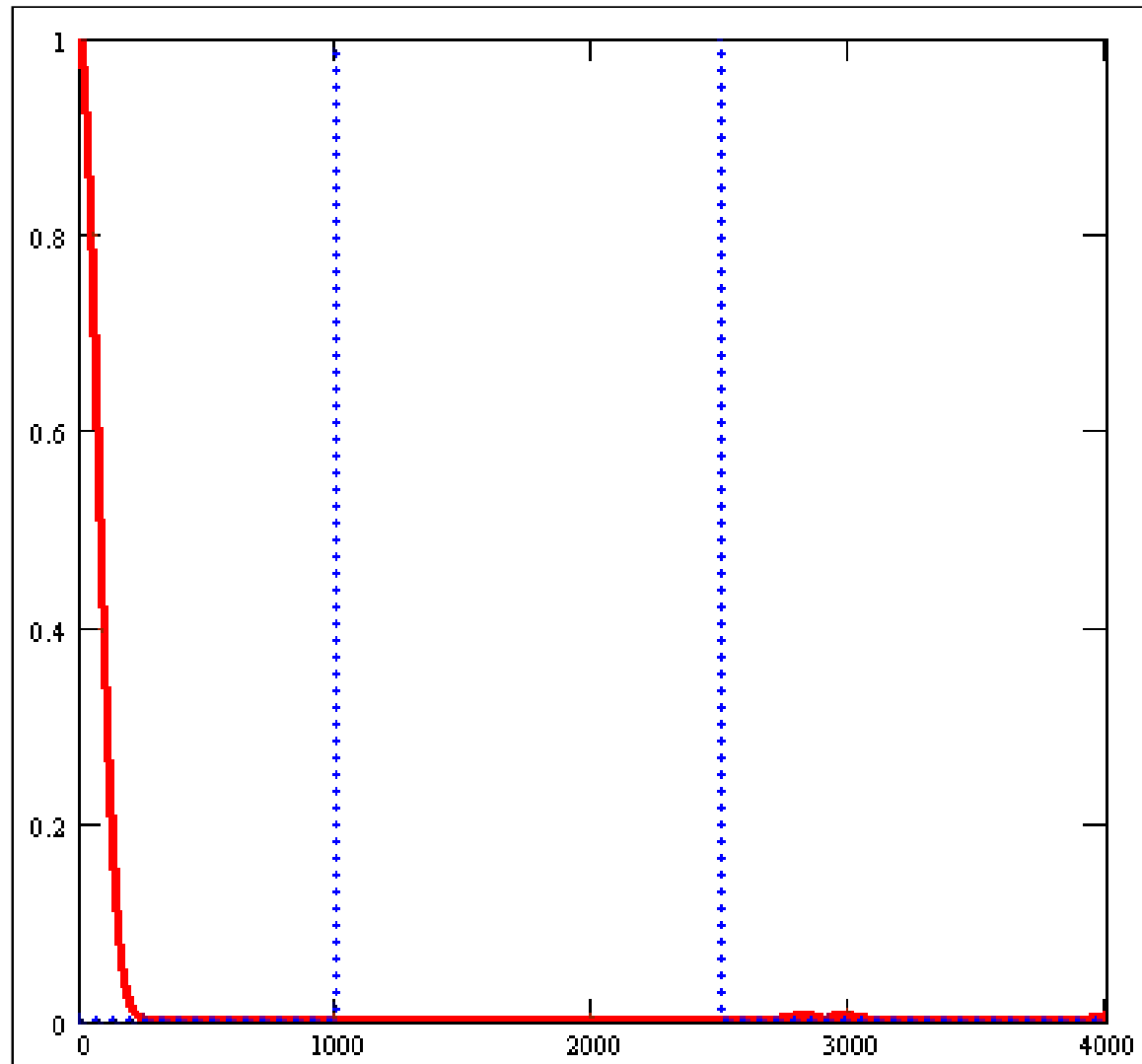
Pulse Propagation through a Slow-Light Medium ($n_g = 2$, $v_g = 0.5 c$)



Pulse Propagation through a Fast-Light Medium ($n_g = .2$, $v_g = 5 c$)

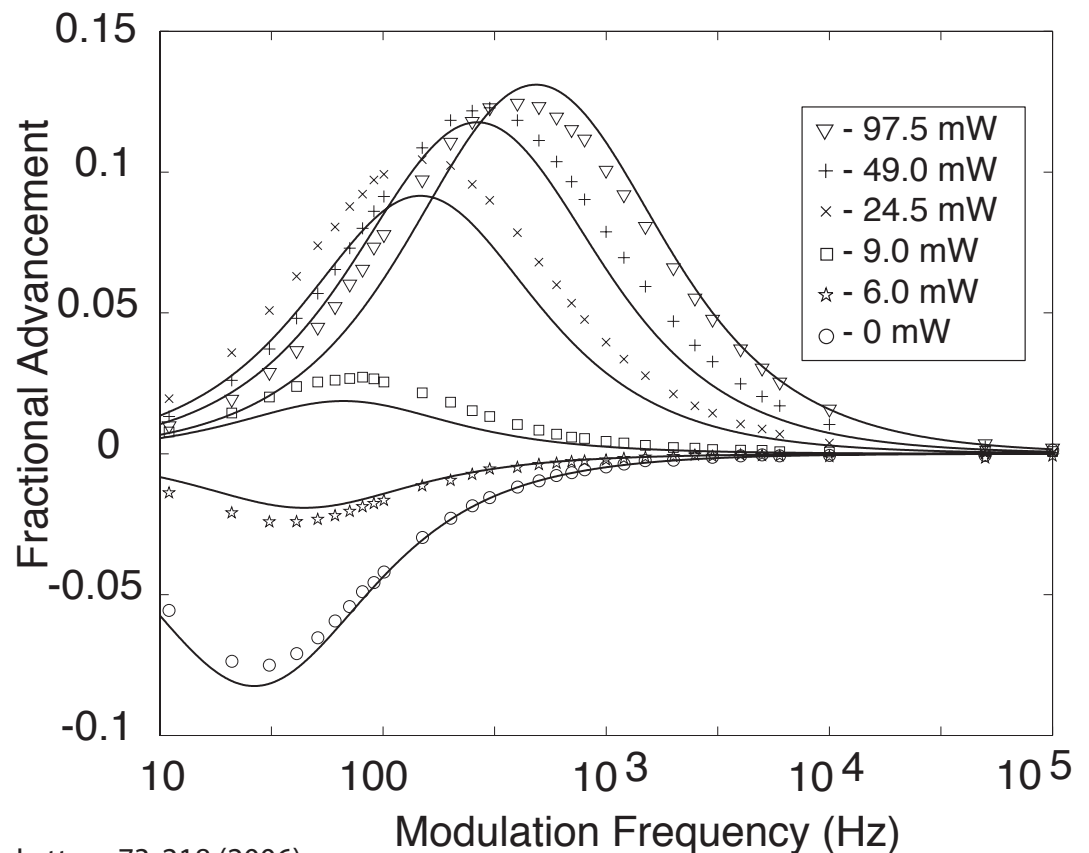
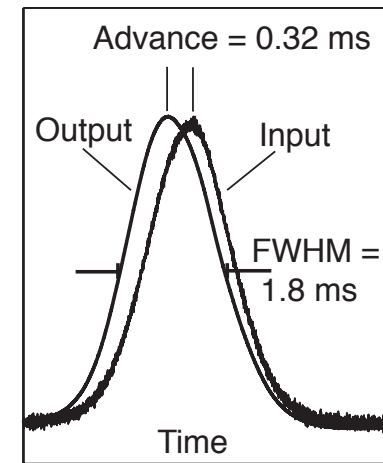
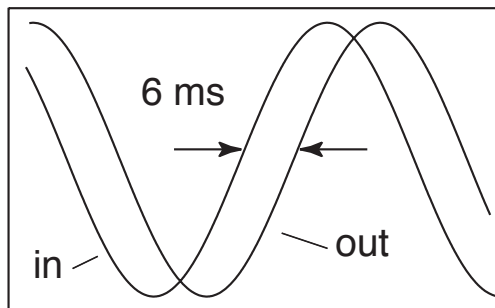
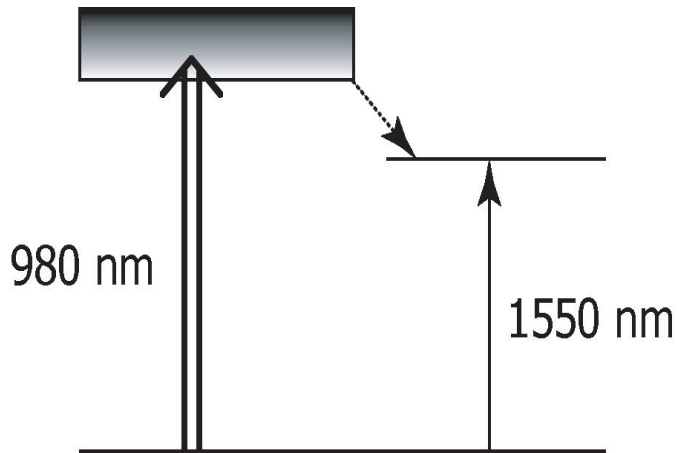


Pulse Propagation through a Fast-Light Medium ($n_g = -.5, v_g = -2 c$)

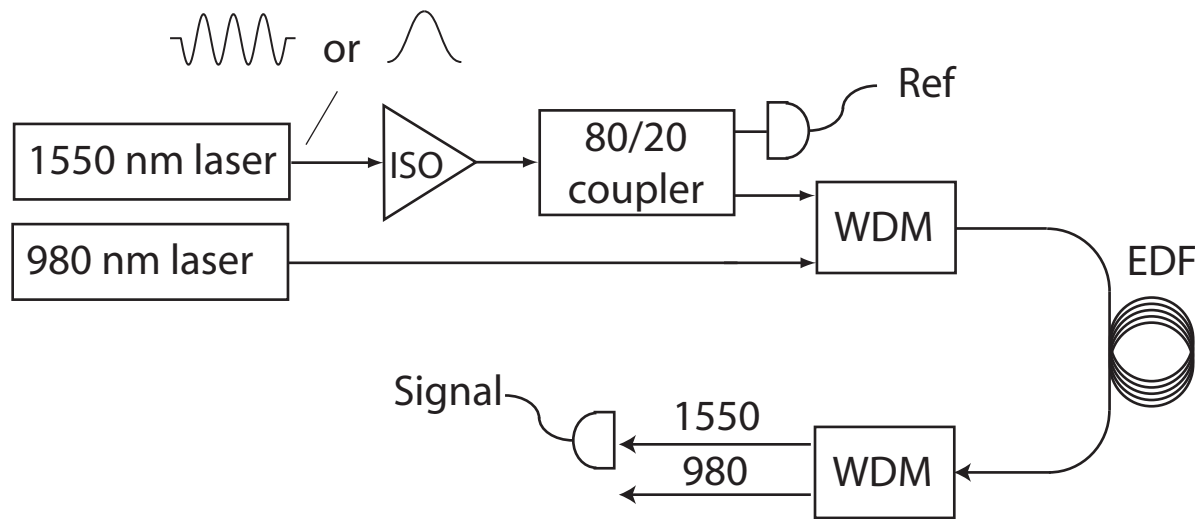


Slow and Fast Light in an Erbium Doped Fiber Amplifier

- Fiber geometry allows long propagation length
- Saturable gain or loss possible depending on pump intensity



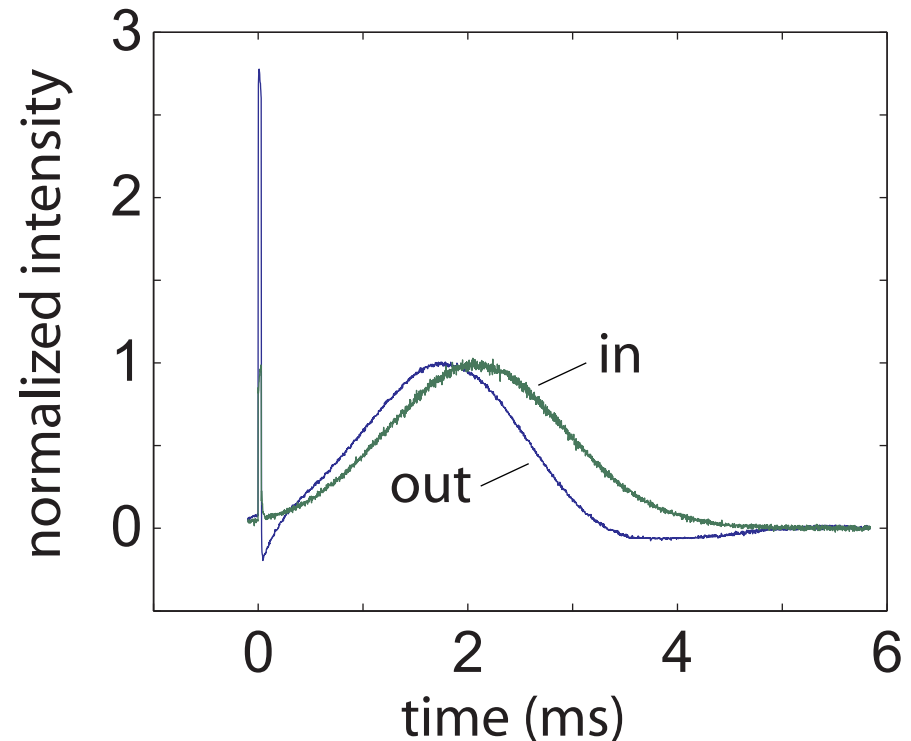
Observation of Backward Pulse Propagation in an Erbium-Doped-Fiber Optical Amplifier



We time-resolve the propagation of the pulse as a function of position along the erbium-doped fiber.

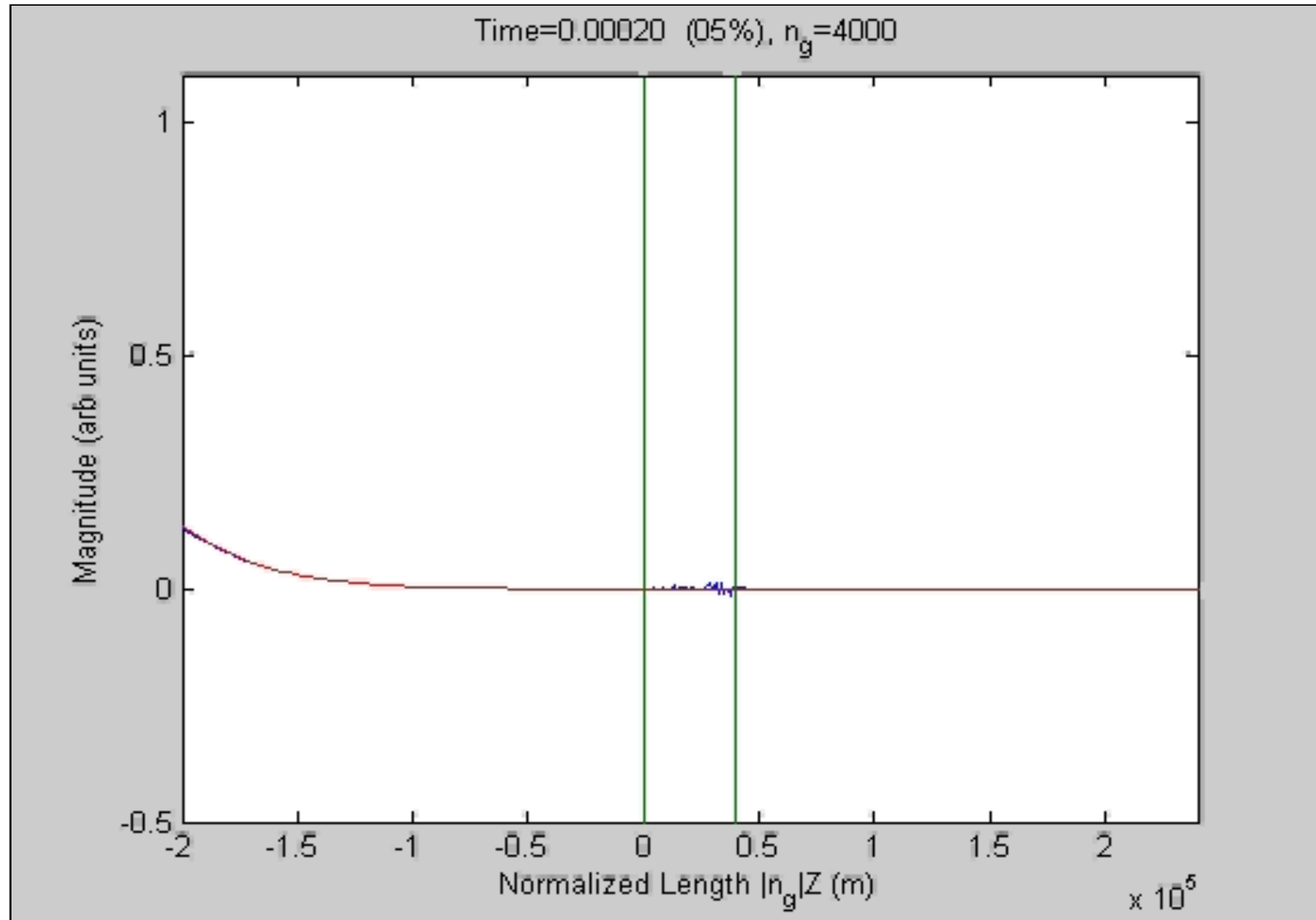
Procedure

- cutback method
- couplers embedded in fiber



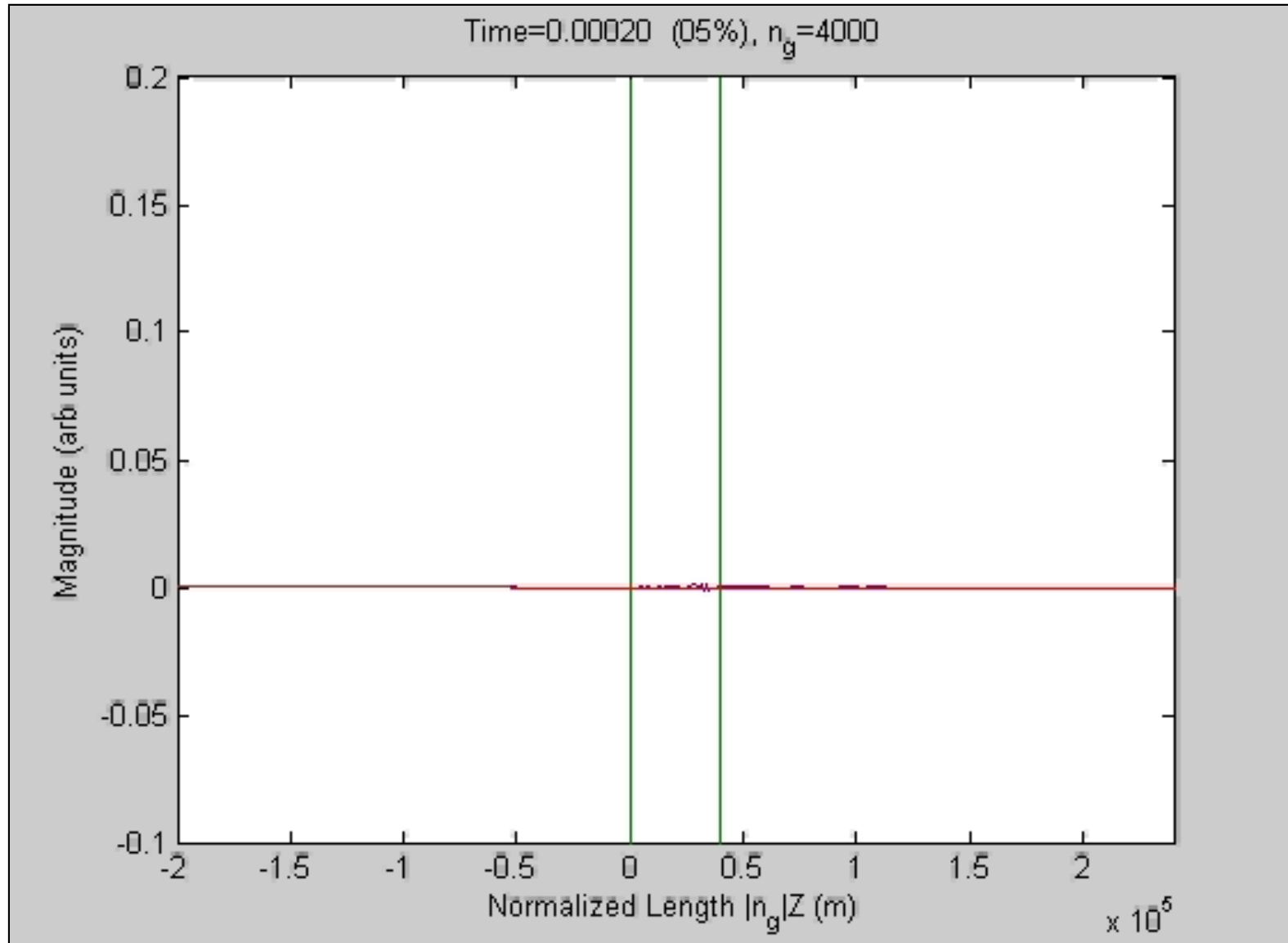
Experimental Results: Backward Propagation in Erbium-Doped Fiber

Normalized: (Amplification removed numerically)



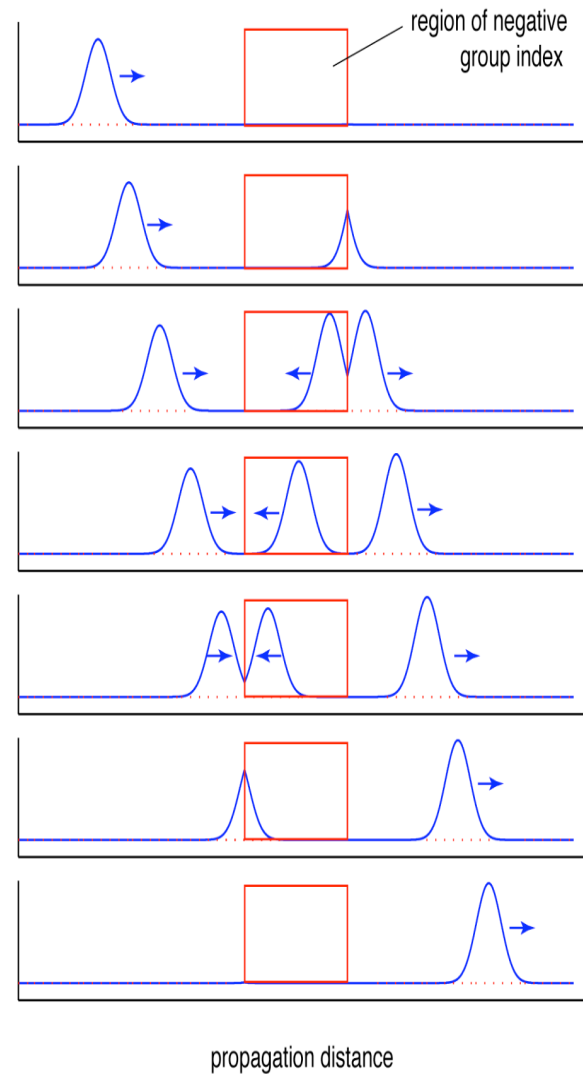
Experimental Results: Backward Propagation in Erbium-Doped Fiber

Un-Normalized

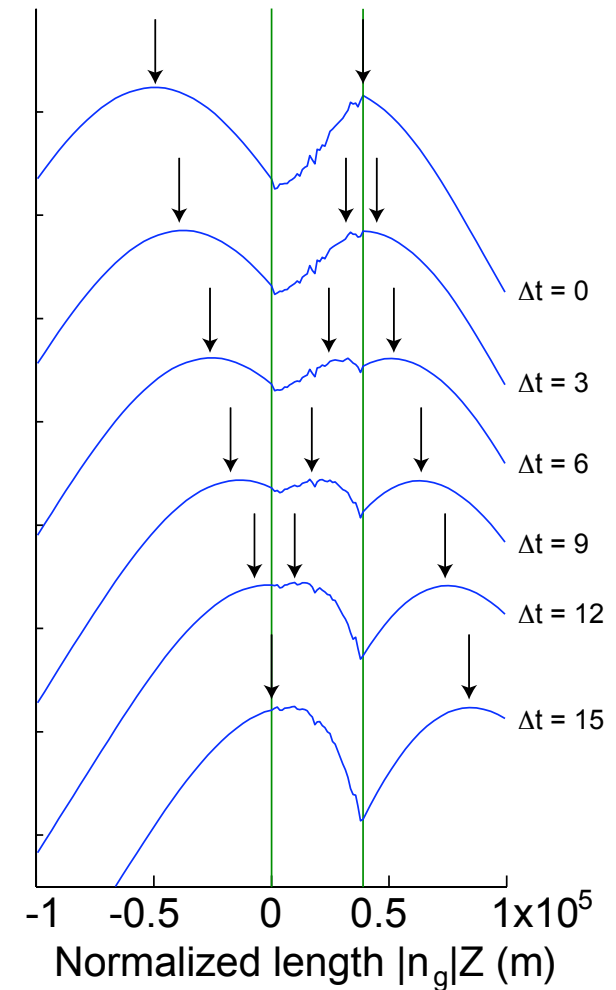


- A strongly counterintuitive phenomenon
- But entirely consistent with established physics
- G. M. Gehring, A. Schweinsberg, C. Barsi, N. Kostinski, and R. W. Boyd, *Science* 312, 985 2006.

- conceptual prediction



- laboratory results



Observation of Backward Pulse Propagation in an Erbium-Doped-Fiber Optical Amplifier

Summary:

“Backwards” propagation is a realizable physical effect.

(Of course, many other workers have measured negative time delays. Our contribution was to measure the pulse evolution within the material medium.)

Causality and Superluminal Signal Transmission

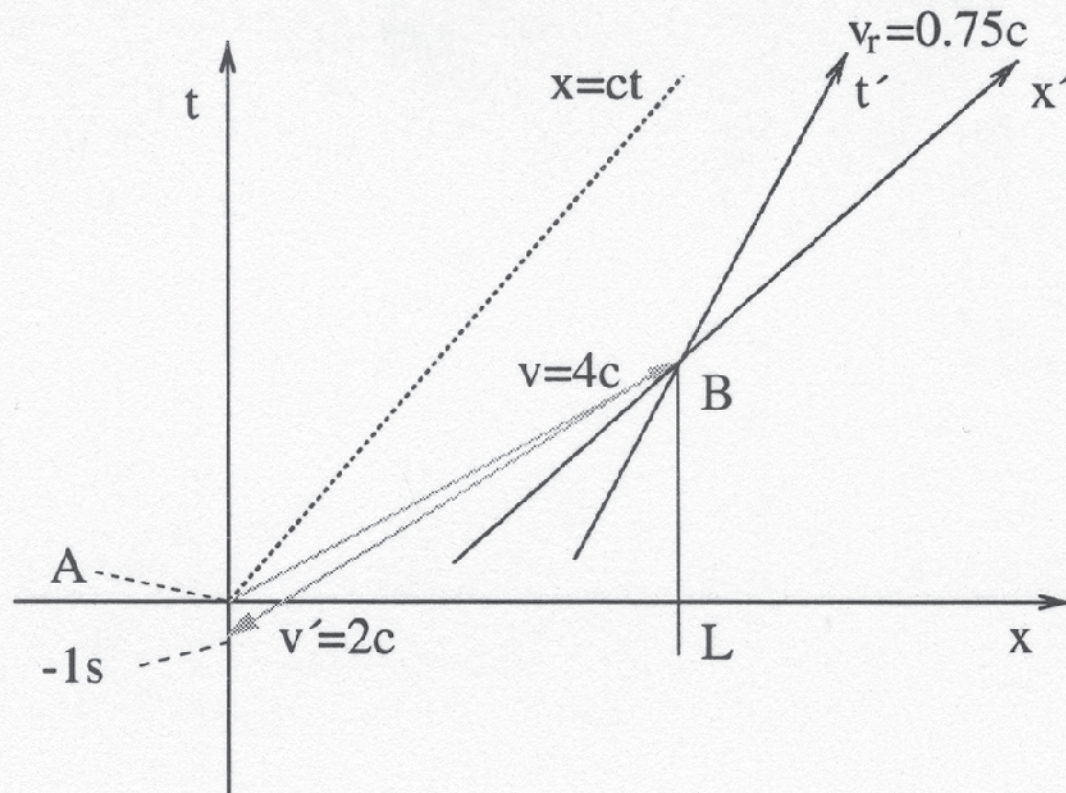
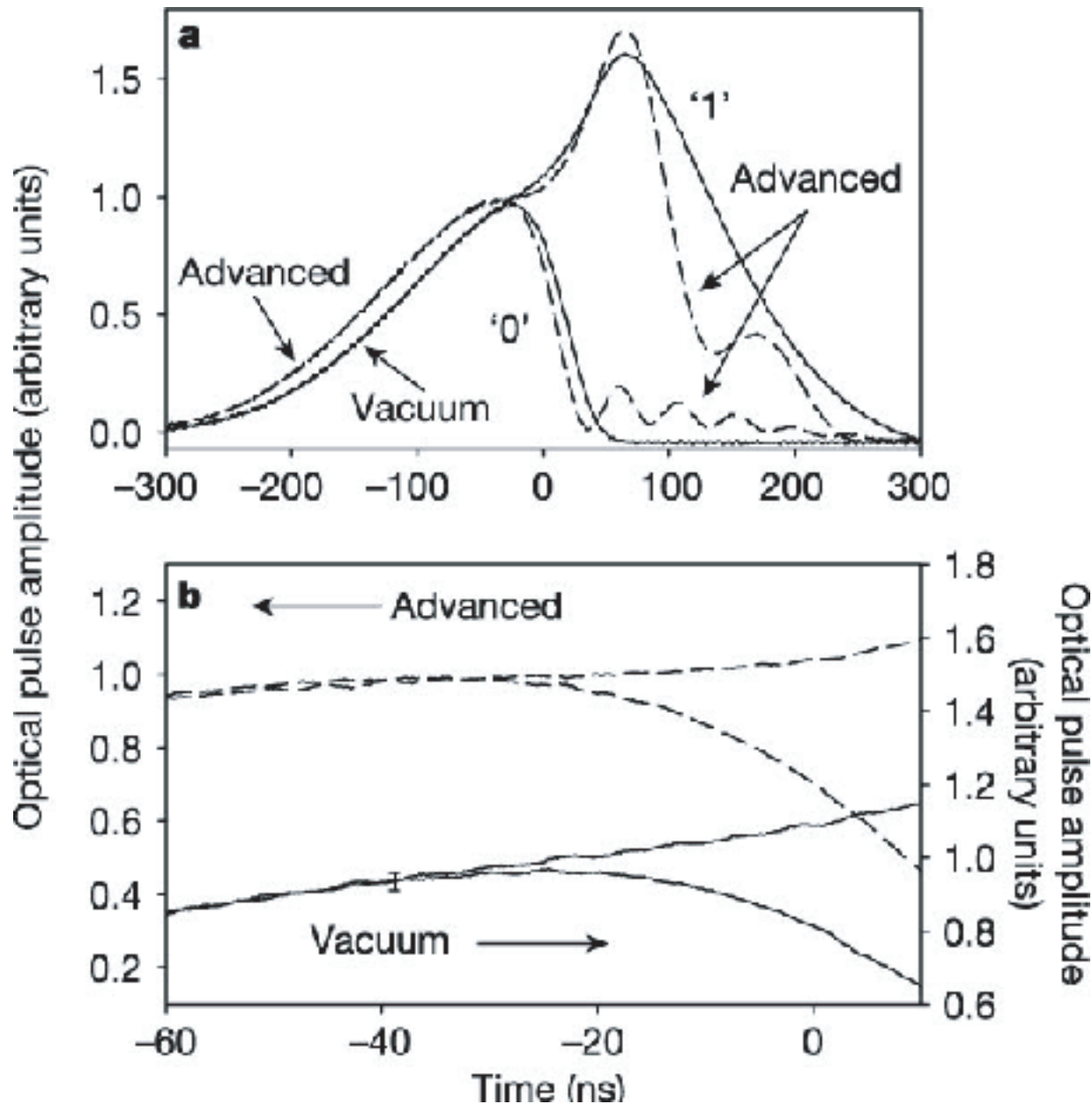


Fig. 6 Coordinates of two inertial observers **A** (0,0) and **B** with $O(x,t)$ and $O'(x',t')$ moving with a relative velocity of $0.75c$. The distance L between **A** and **B** is 2000000 km. **A** makes use of a signal velocity $v_s = 4c$ and **B** makes use of $v'_s = 2c$. The numbers in the example are chosen arbitrarily. The signal returns -1 s in the past in **A**.

Information Velocity in a Fast Light Medium

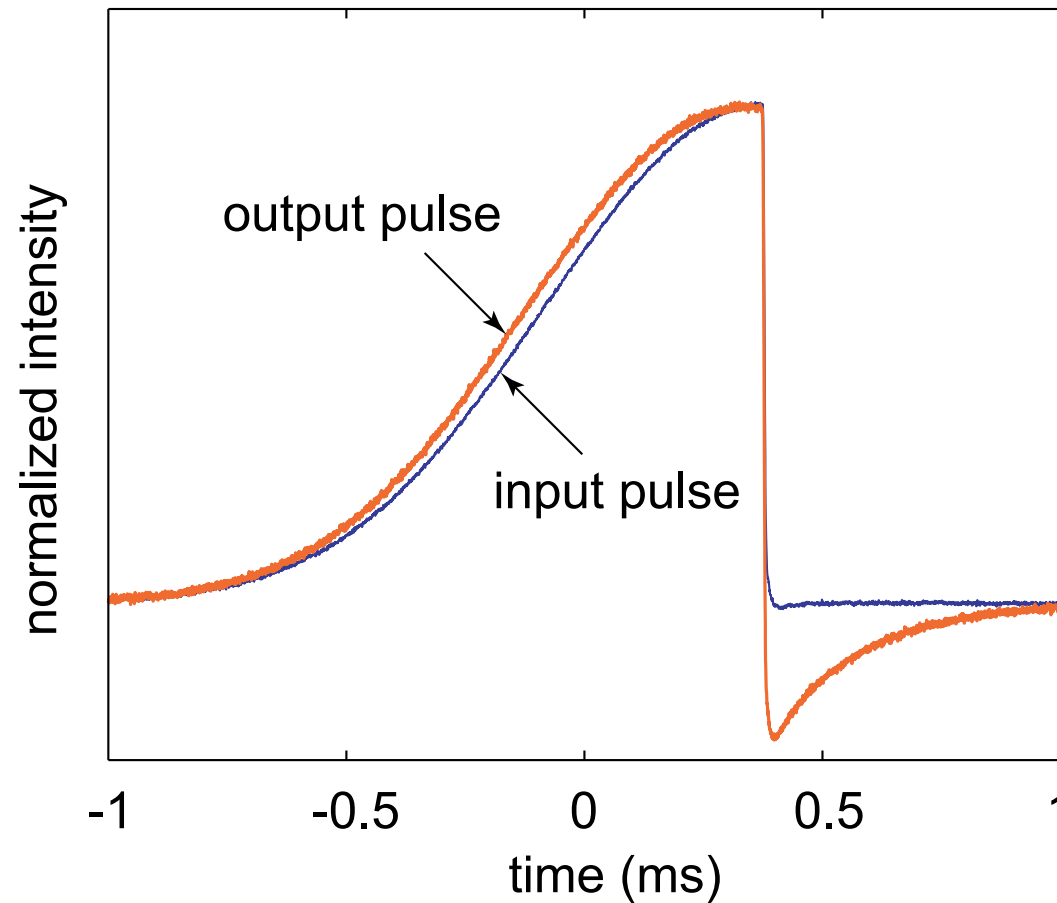


M.D. Stenner, D.J. Gauthier, and M.I. Neifeld, *Nature*, 425 695 (2003).

Pulses are not distinguishable "early."

$$v_i \leq c$$

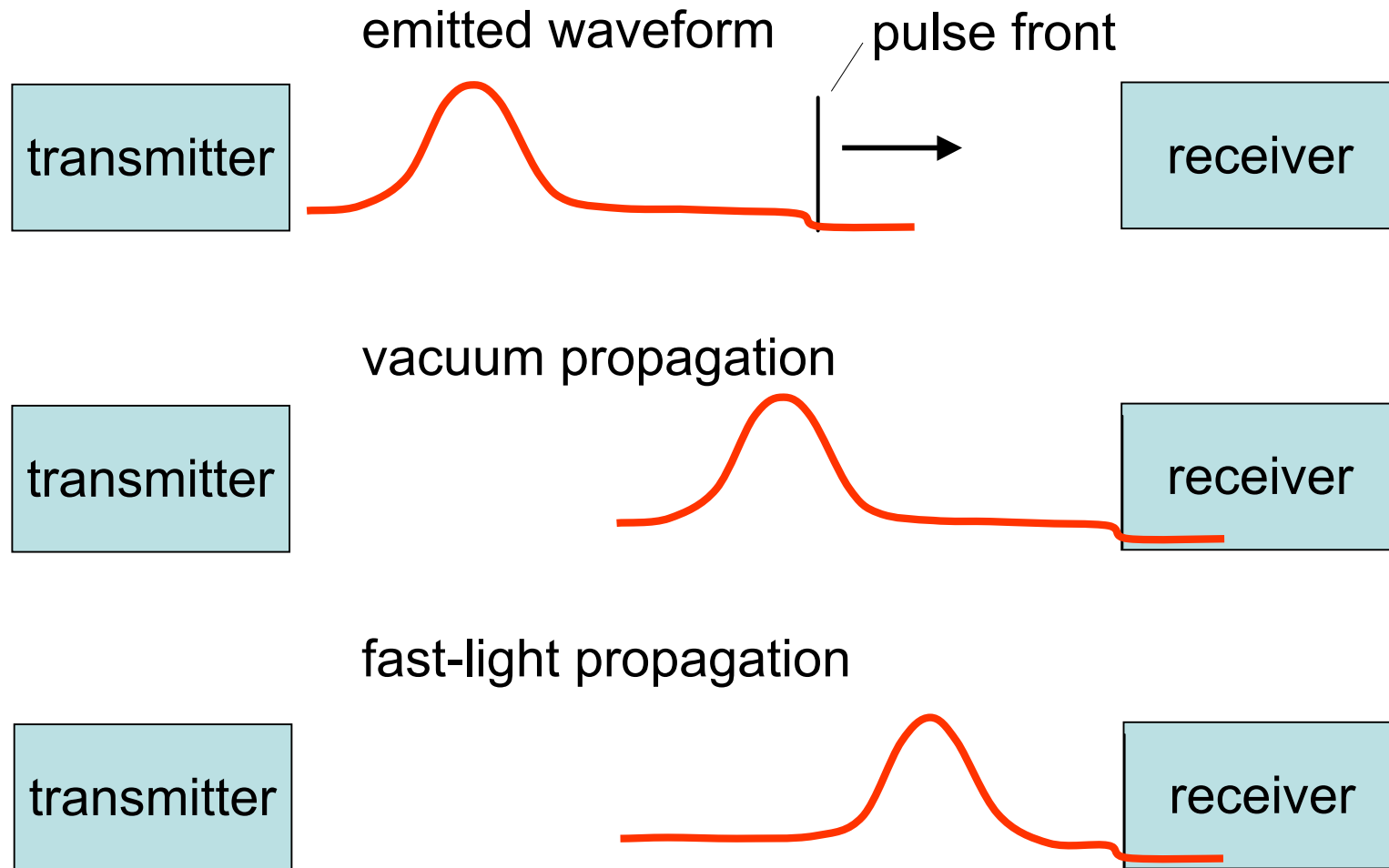
Propagation of a Truncated Pulse through Alexandrite as a Fast-Light Medium



Smooth part of pulse propagates at group velocity

Discontinuity propagates at phase velocity

How to Reconcile Superluminality with Causality



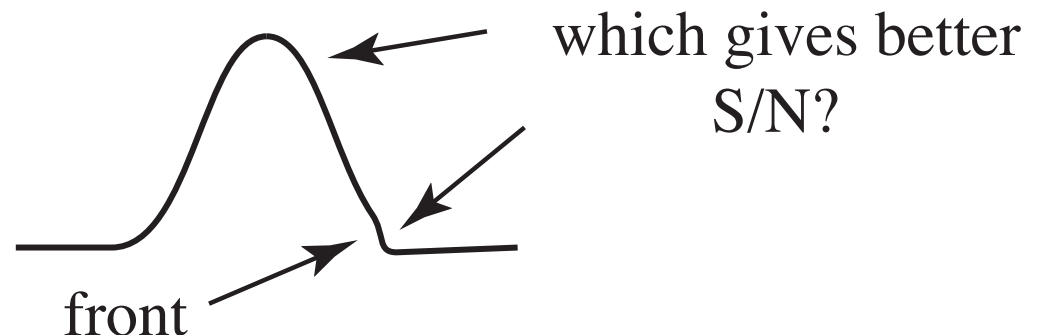
Information Velocity – Tentative Conclusions

In principle, the information velocity is equal to c for both slow- and fast-light situations. **So why is slow and fast light even useful?**

Because in many practical situations, we can perform reliable measurements of the information content only near the peak of the pulse.

In this sense, useful information often propagates at the group velocity.

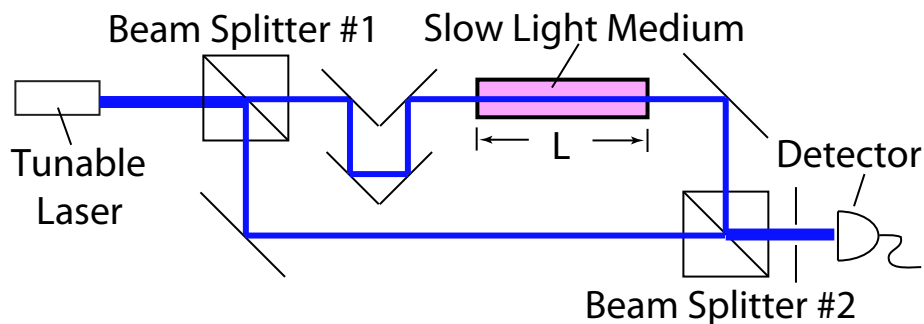
In a real communication system it would be really stupid to transmit pulses containing so much energy that one can reliably detect the very early leading edge of the pulse.



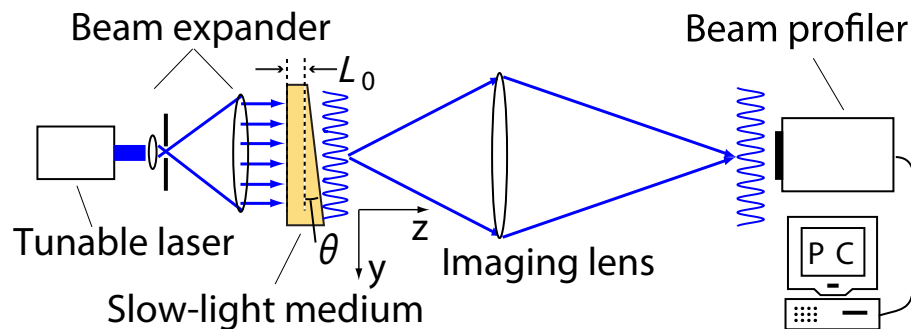
Interferometry and Slow Light

- Under certain (but not all) circumstances, the sensitivity of an interferometer is increased by the group index of the material within the interferometer!
- Sensitivity of a spectroscopic interferometer is increased

Typical interferometer:



We use $\text{CdS}_x\text{Se}_{1-x}$ as our slow-light medium

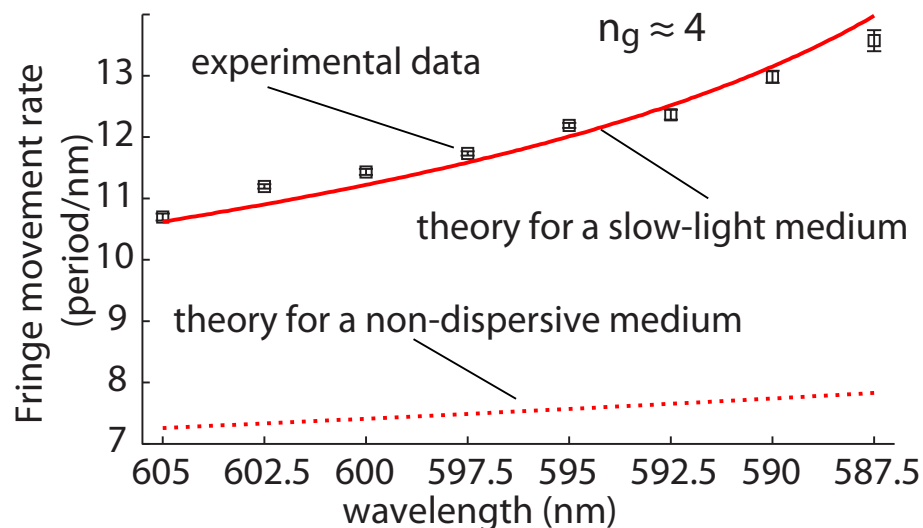


Here is why it works:

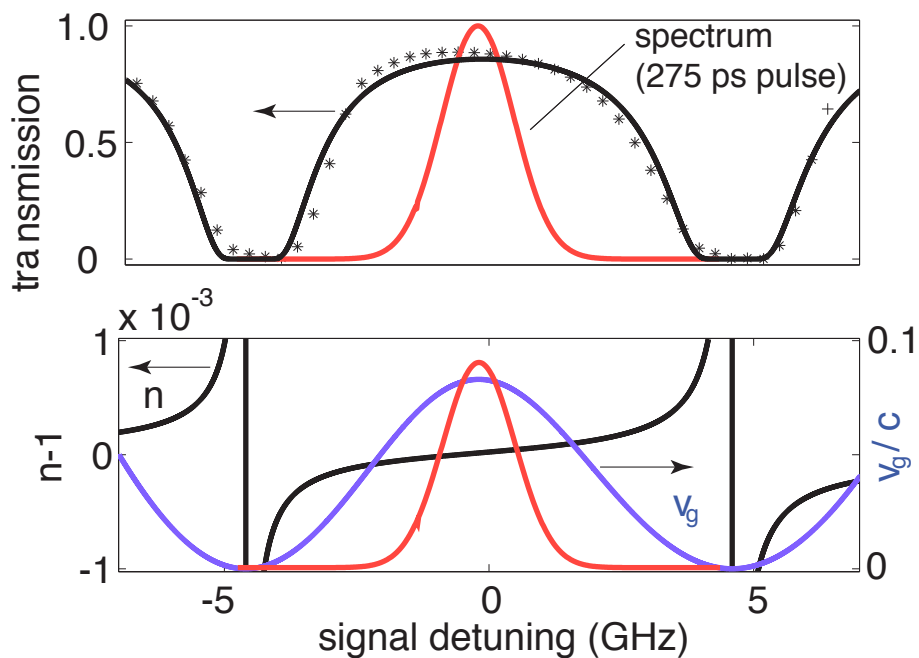
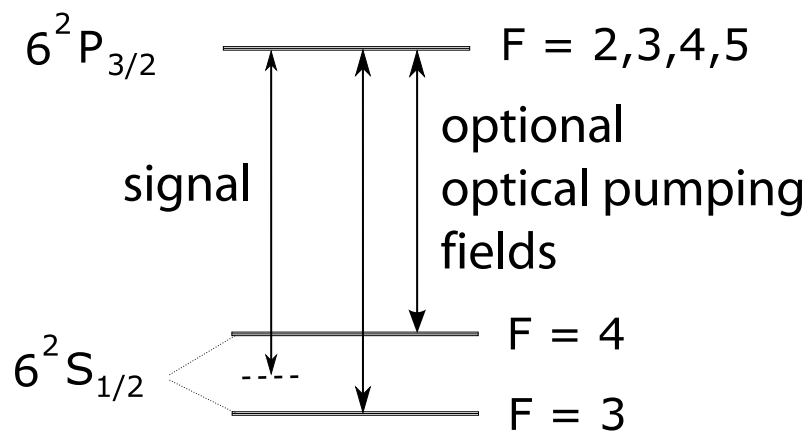
$$\frac{d\Delta\phi}{d\omega} = \frac{d}{d\omega} \left(\frac{\omega n L}{c} \right) = \frac{L}{c} \left(n + \omega \frac{dn}{d\omega} \right) = \frac{L n_g}{c}$$

Shih et al, Opt. Lett. 2007

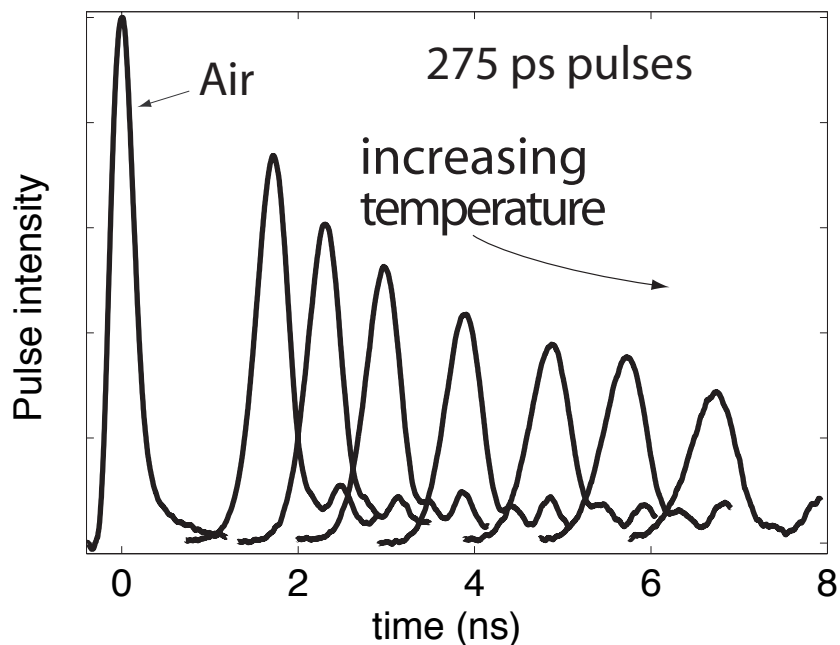
Our experimental results



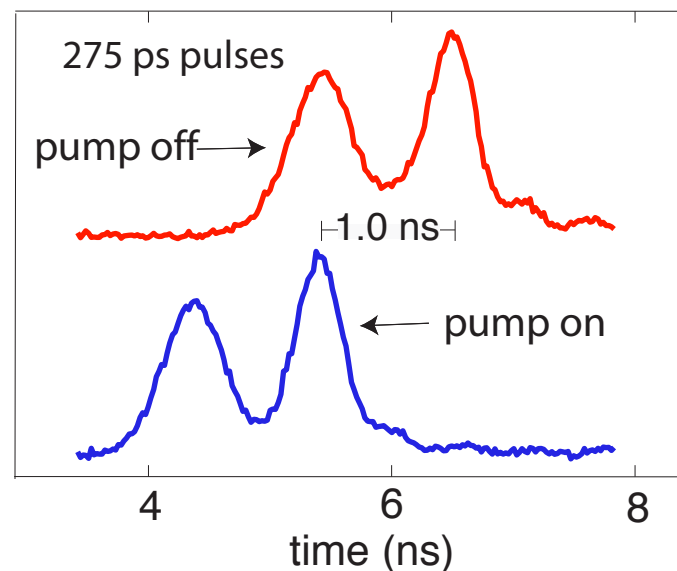
Tunable Delays of up to 80 Pulse Widths in Atomic Cesium Vapor



- coarse tuning: temperature



- fine tuning: optical pumping



Tunable Delays of up to 80 Pulse Widths in Atomic Cesium Vapor

Comment: In EIT based slow light, spectral reshaping is the dominant limitation. But far off resonance, this effect is negligible. Group velocity dispersion becomes important.

Longer input pulses lead to reduced gvd distortion and longer fractional delays

Results for 740 ps pulses

